

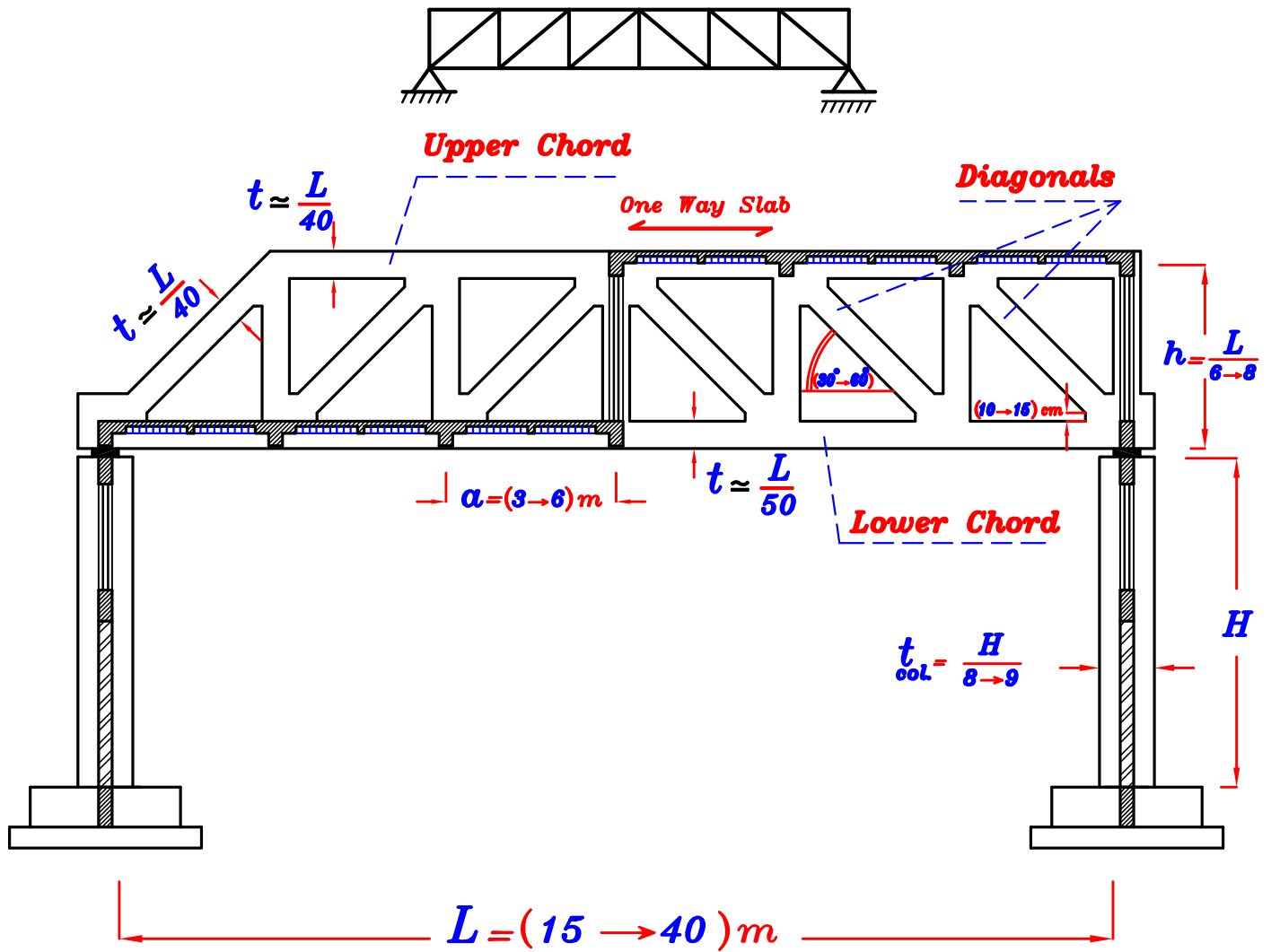
Truss & Vierendeel.

نسألكم الدعاء

Truss & Vierendeel. Table of Contents.

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Trusses



* **Span** (L) = $(15 \rightarrow 40) m$

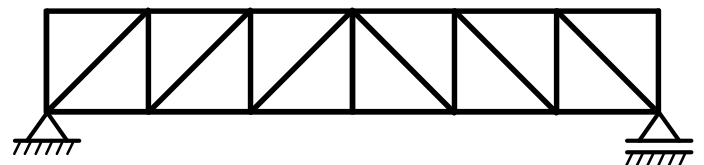
* **Height** (h) = $\frac{L}{6 \rightarrow 8}$

* t (Compression members) $\approx \frac{L}{40}$

* t (Tension members) $\approx \frac{L}{50}$

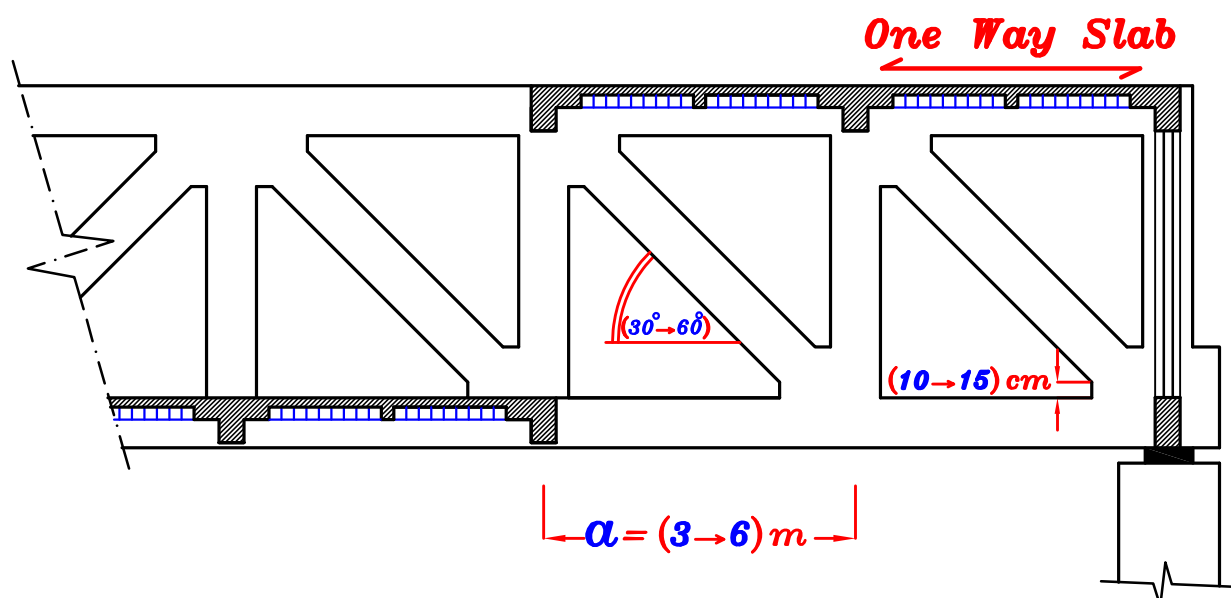
* $b = 0.30 m$ } **الأكبر**
 $\frac{\text{Spacing}}{20}$

* $t_{col} = \frac{H}{8 \rightarrow 9}$



Static System

- يجب أن تكون كل الاحمال مركزه عند ال **Joints** فقط و لكى نتحكم فى ذلك يجب أن :
- ١- نضع كل الكمرات المحموله على ال **Truss** عند ال **Joints** فقط .
 - ٢- نأخذ كل البلاطات **One Way Slabs** فى إتجاه الكمرات بحيث لا ترمى أى أحمال على ال **Truss** (عاده تؤخذ **One Way H.B. slab**).
 - ٣- نفرض أن ال **O.W.** لل **Truss** يؤثر كأنه **Concentrated Load** عند ال **Joints**.



لتحديد نوع القوى (شد أو ضغط) فى ال **members** يكون حسب شكل ال **B.M.** و شكل ال **Truss**.

Upper & Lower Chord *

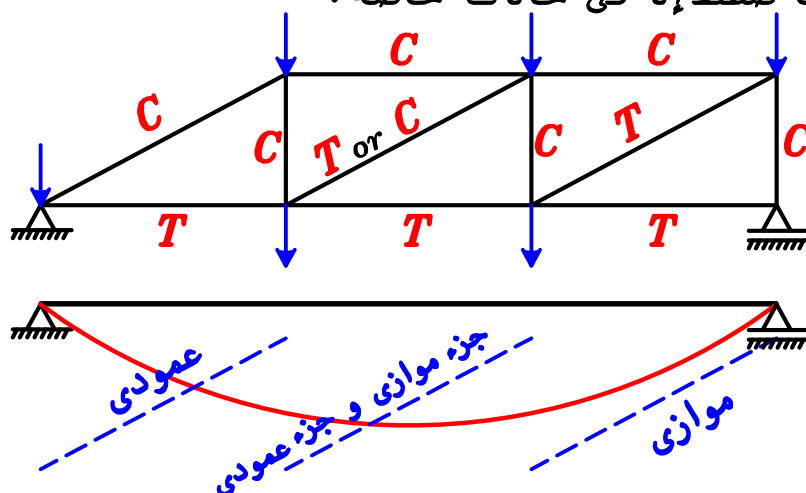
- إذا كان ال **member** فى نفس إتجاه ال **B.M.** يكون عليه شد .
- إذا كان ال **member** عكس إتجاه ال **B.M.** يكون عليه ضغط .

Diagonal members *

- إذا كان ال **member** موازى لل **moment** يكون عليه شد .
- إذا كان ال **member** عمودى على ال **moment** يكون عليه ضغط .

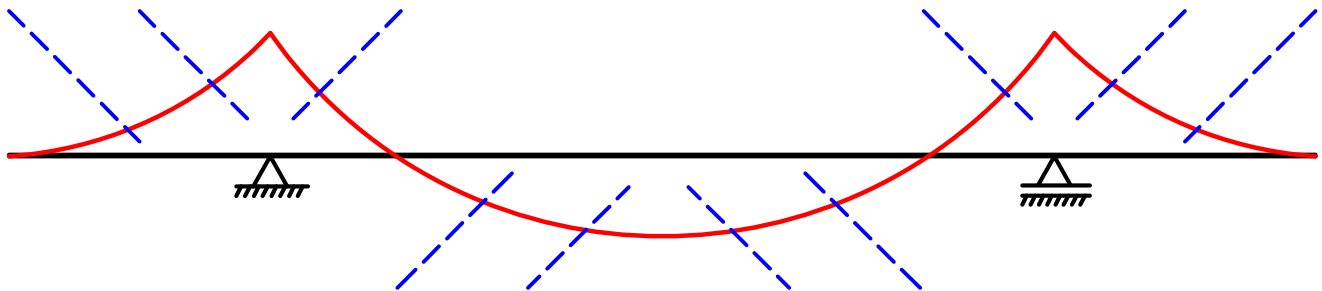
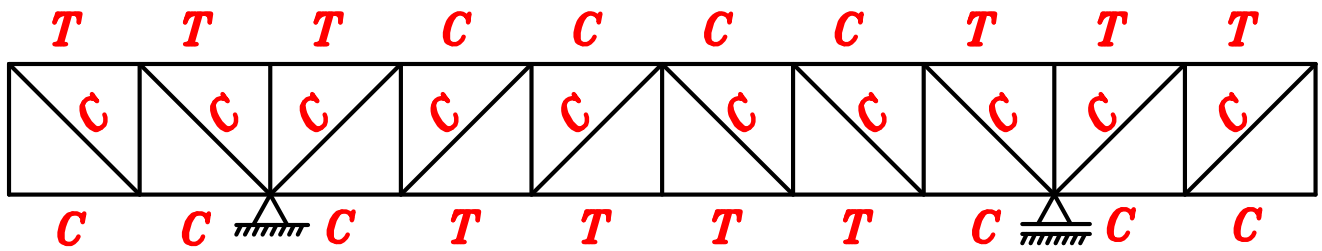
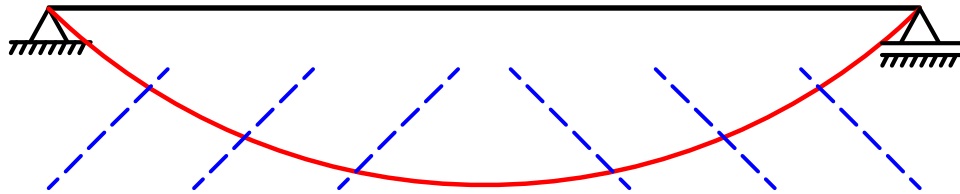
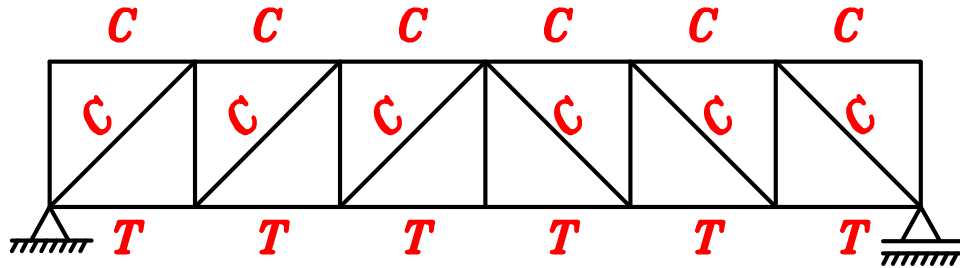
Vertical members *

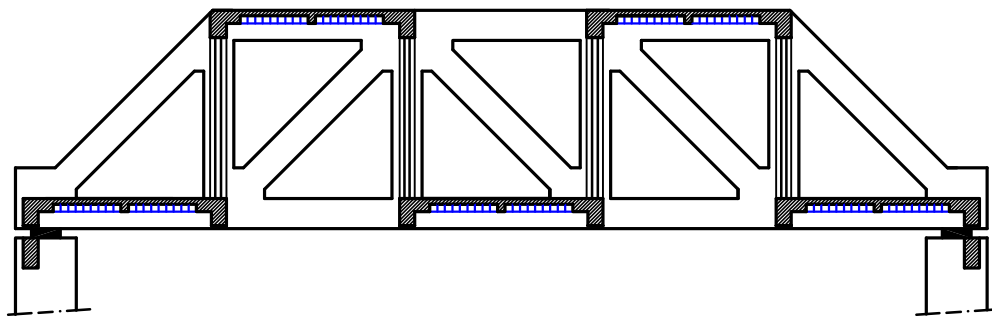
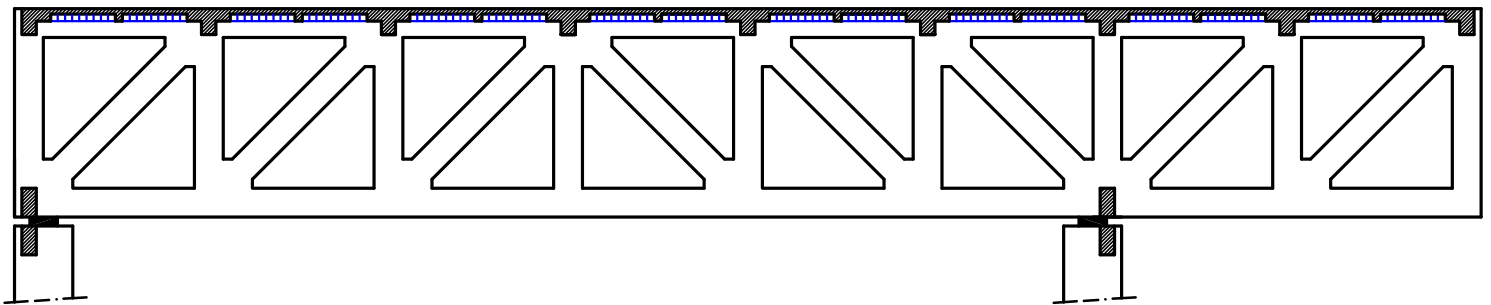
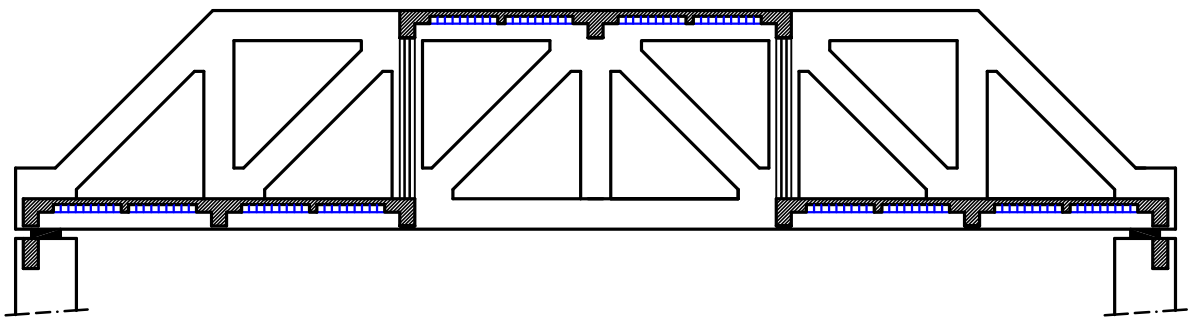
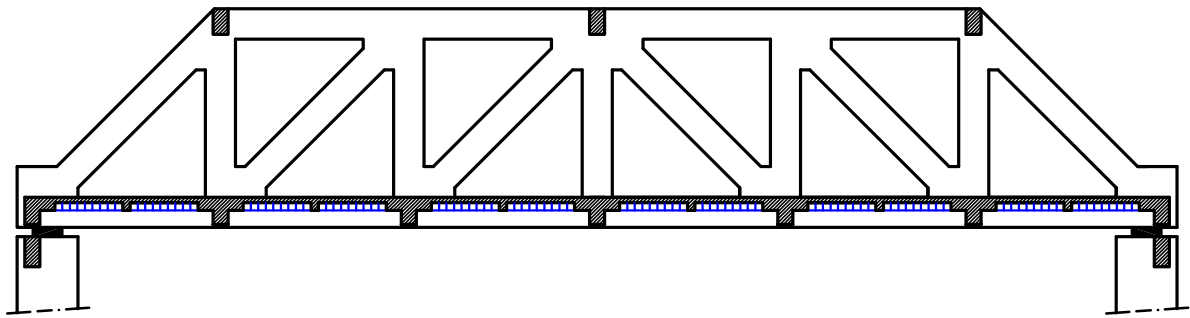
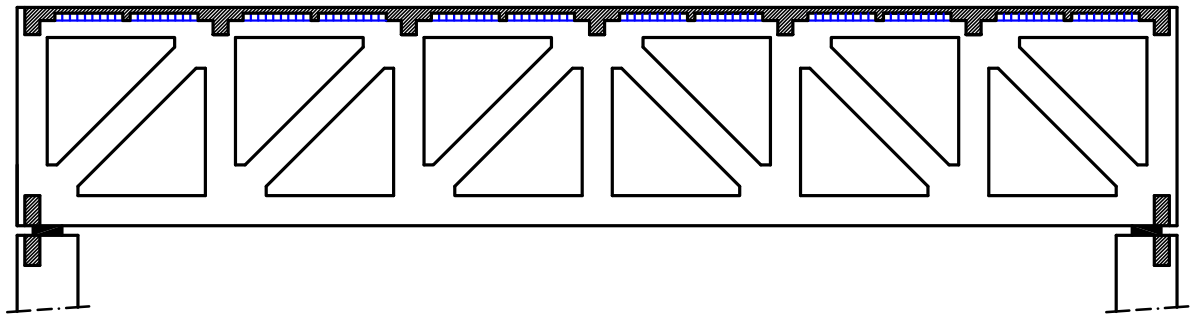
عاده يكون عليها ضغط إلا فى حالات خاصه .

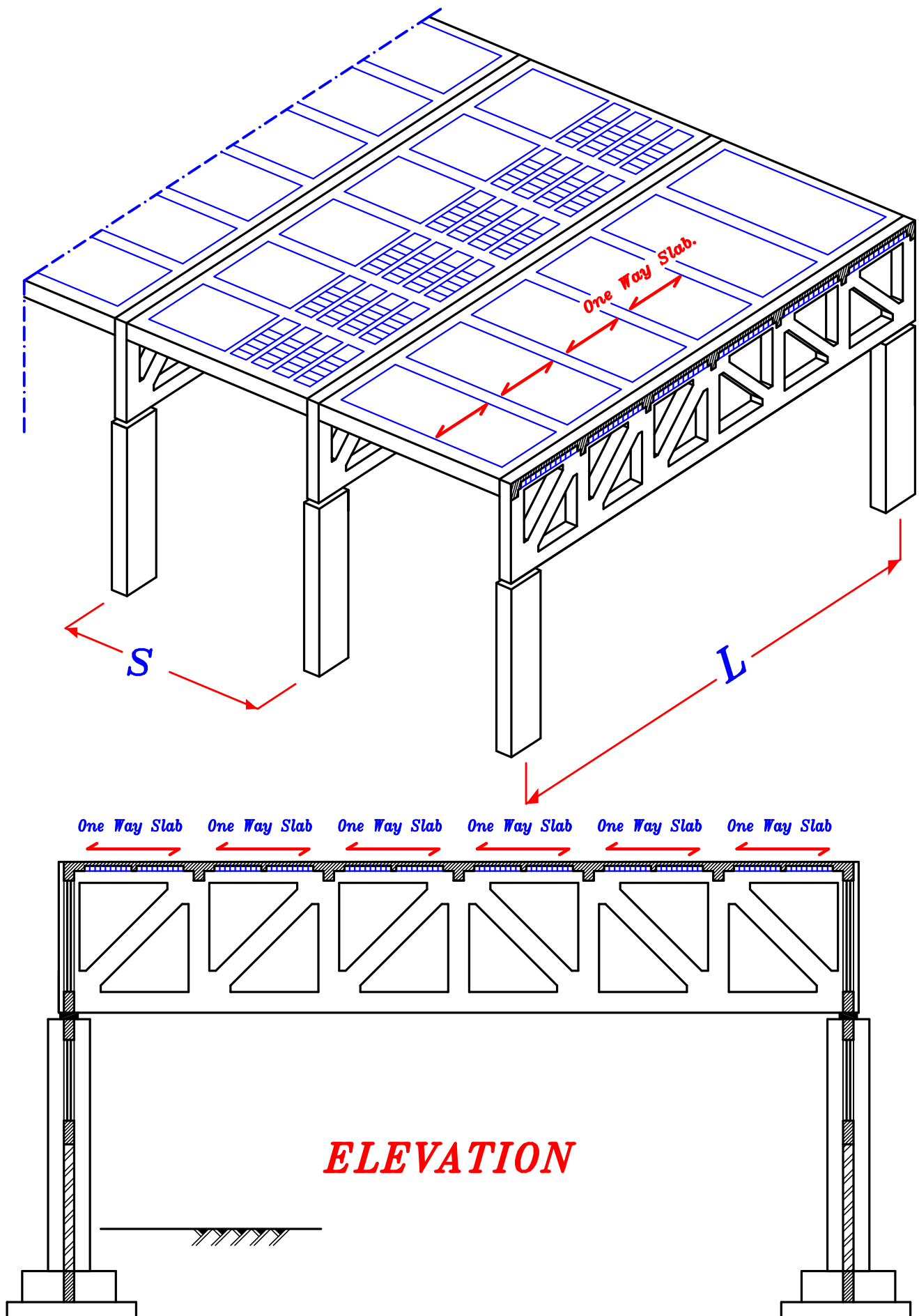


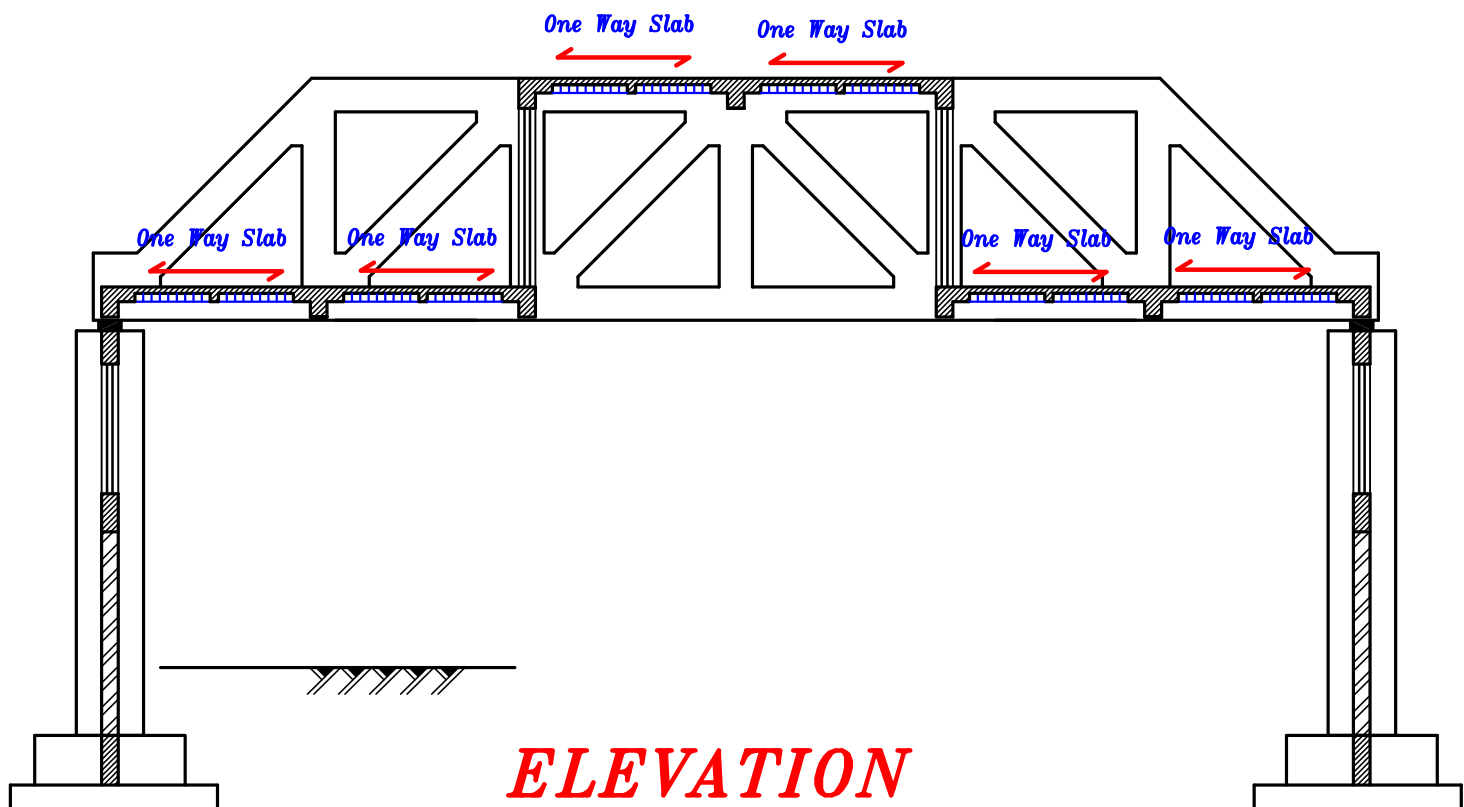
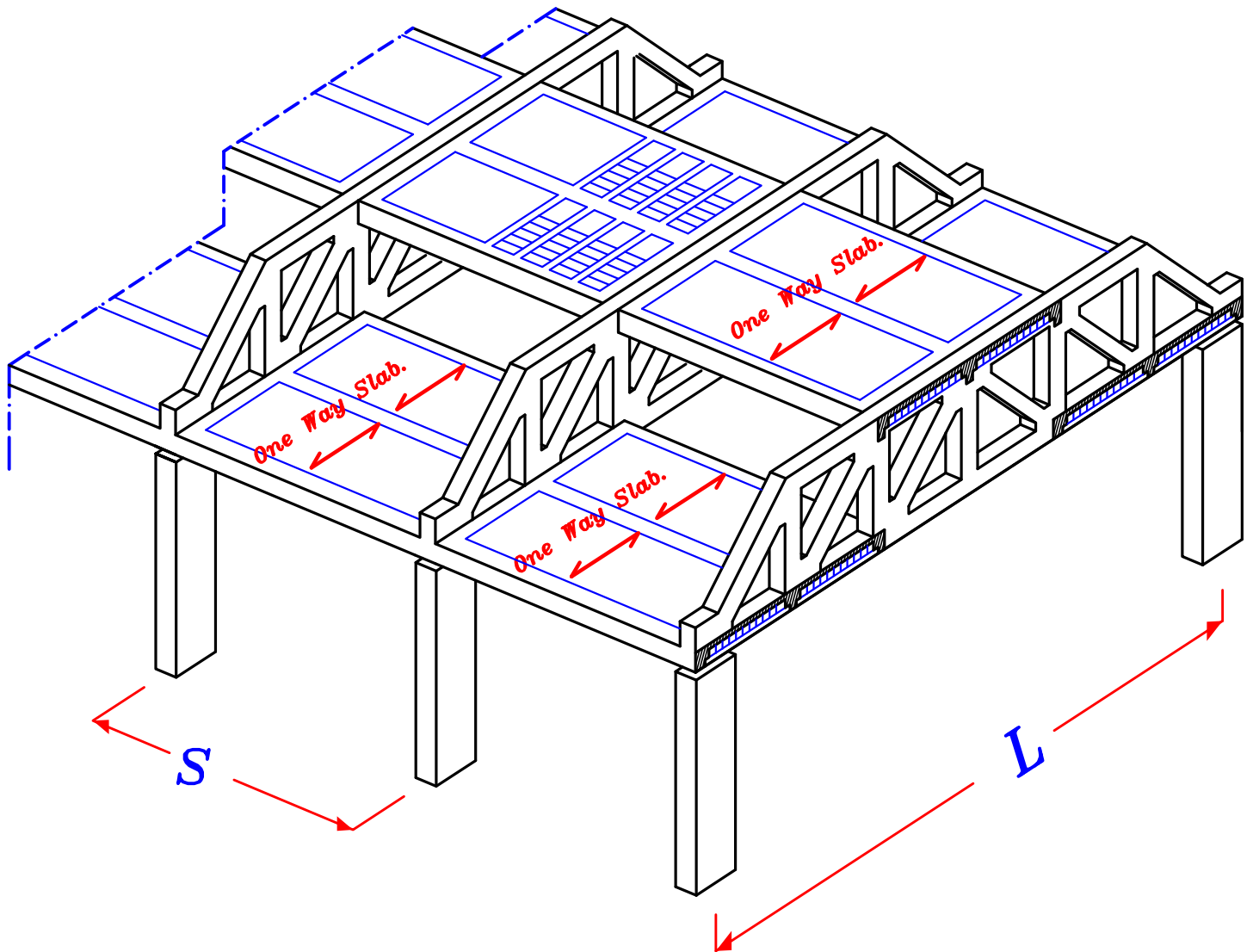
حيث أن الخرسانه أفضل فى الضغط من الشد (عكس ال *Steel*)

∴ فمن المفضل وضع ال *Diagonal members* عمودية على شكل ال *B.M.* لكى تكون معرضه للضغط .







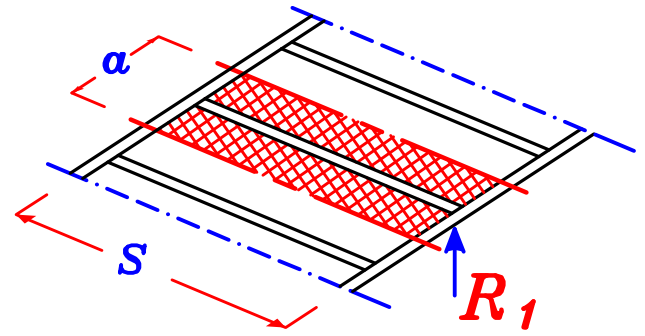


Loads on Truss.

① Get Loads on Beam B_1

$$w_1 = O.W._{(beam)} + \left(\frac{w_{rib}}{S} \right) * a$$

$$R_1 = w_1 * S$$



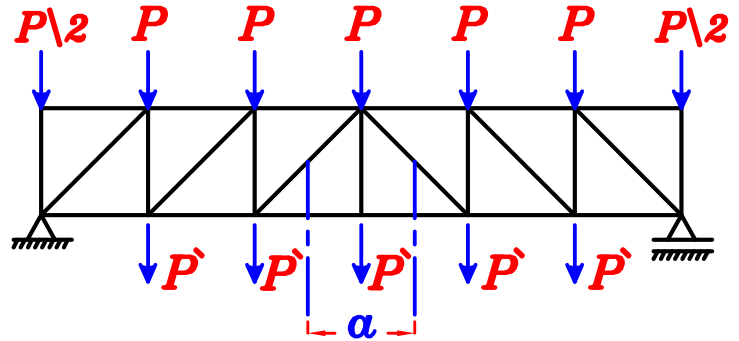
② Take

$O.W. (Truss)$

$$\cong 17.5 \text{ kN/m (U.L.)}$$

$$P' = \frac{0.w.*a}{2} = \checkmark \text{ kN}$$

$$P = P' + R_1 = \checkmark \text{ kN}$$



③ Solve the Truss, By using.

Computer or method of sections or Joints equilibrium.

Then get N.F. on all members.

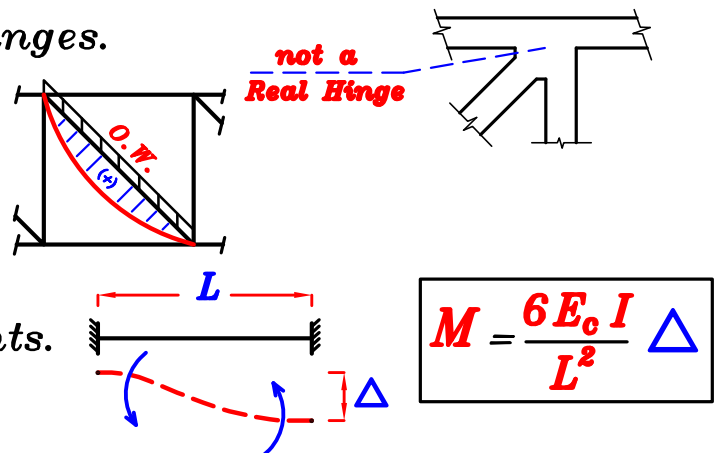
④ Design the Members.

توجد عزوم على ال members المختلفة نتیجه

Ⓐ The joints are not a Real Hinges.

Ⓑ Due to O.W. of the member.

Ⓒ Relative Displacement of joints.



لذلك عند تصميم ال members المختلفة نأخذ قيمه moment صغيره

$$\text{Take } M = \checkmark \text{ kN.m} \xrightarrow{\text{From}} \frac{e}{t} \cong \underset{\checkmark}{0.1} \longrightarrow 0.2$$

Ⓐ Design of Compression members.

Designed on ***N, M***

N From calculation of Truss

M From $\frac{e}{t} \simeq 0.1 \xrightarrow{\checkmark\checkmark} 0.2$ } Use I.D.

$$\left. \begin{array}{l} \frac{N}{F_{cu} b t} \\ \frac{e}{t} \simeq 0.1 \end{array} \right\} \text{Get } \rho \quad \mu = \rho * F_{cu} * 10^{-4}$$

$$A_s = A_{s'} = \mu b t$$

IF $\rho < 1.0$ Take $\rho = 1.0$ $2\phi 12 \setminus 25 \text{ cm}$

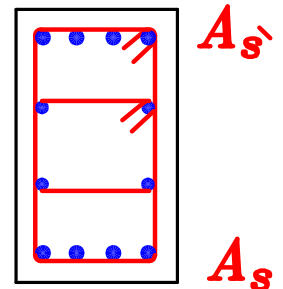
– Check $A_{s_{min.}}$ $2\phi 12 \setminus 25 \text{ cm}$

Calculate $A_{s_{Total}} = A_s + A_{s'}$

Calculate $A_{s_{min.}} = \frac{0.6}{100} * b * t$

IF $A_{s_{Total}} \geq A_{s_{min.}} \therefore \text{o.k.}$

IF $A_{s_{Total}} < A_{s_{min.}}$ take $A_s = A_{s'} = \frac{A_{s_{min.}}}{2}$



Ⓑ Design of Tension members.

Designed on ***T, M***

T From calculation of Truss

M From $\frac{e}{t} \simeq 0.1 \xrightarrow{\checkmark\checkmark} 0.2$

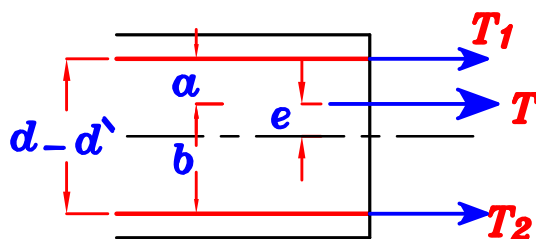
$$e \simeq 0.1 t$$

$$a = \frac{t}{2} - c - e$$

$$b = \frac{t}{2} + c + e$$

$$T_1 = \frac{b}{a+b} * T$$

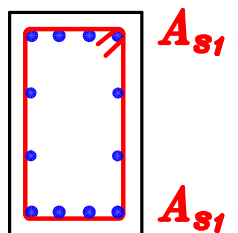
$$A_{s1} = \frac{T_1}{F_y \setminus \delta_s}$$



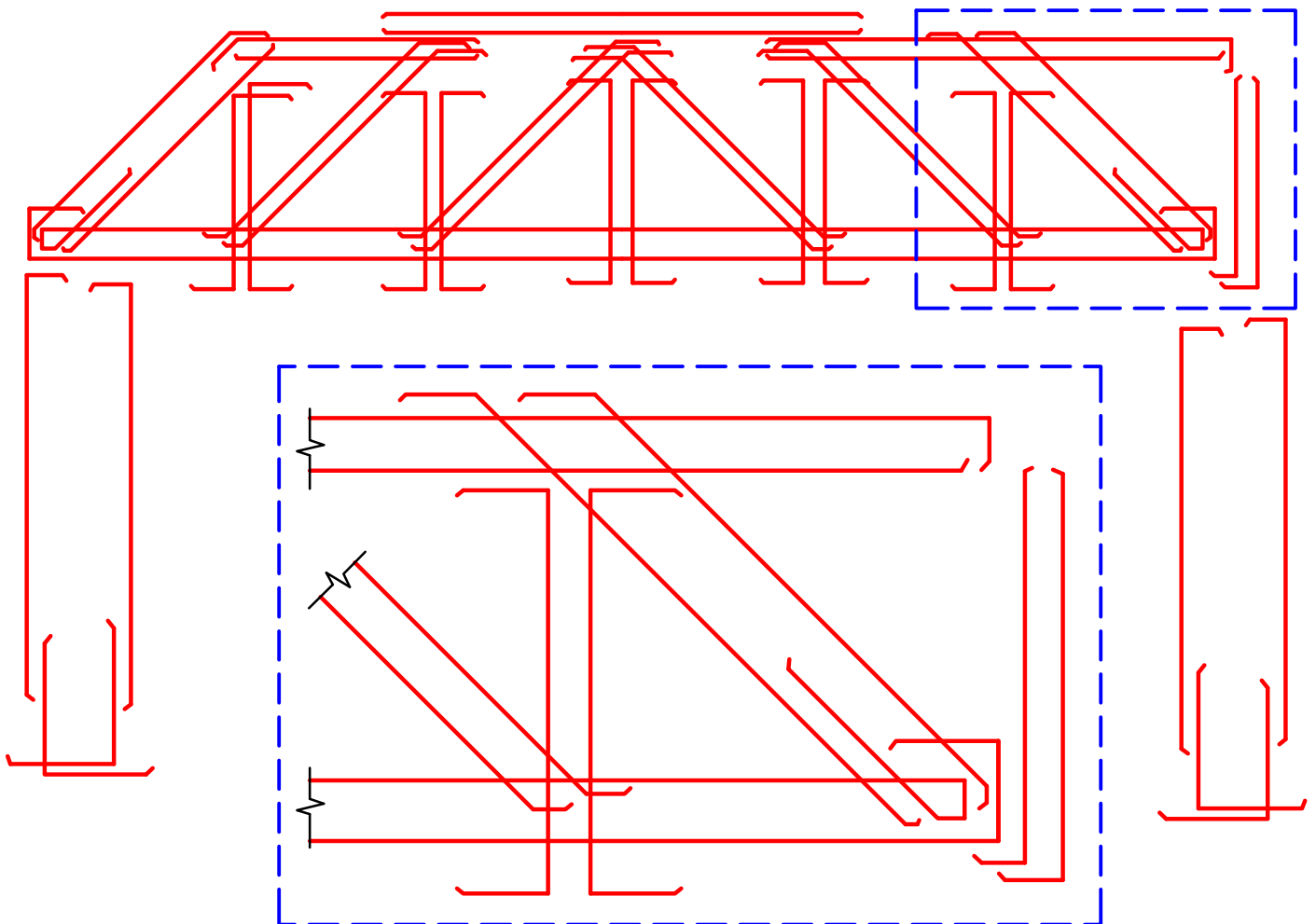
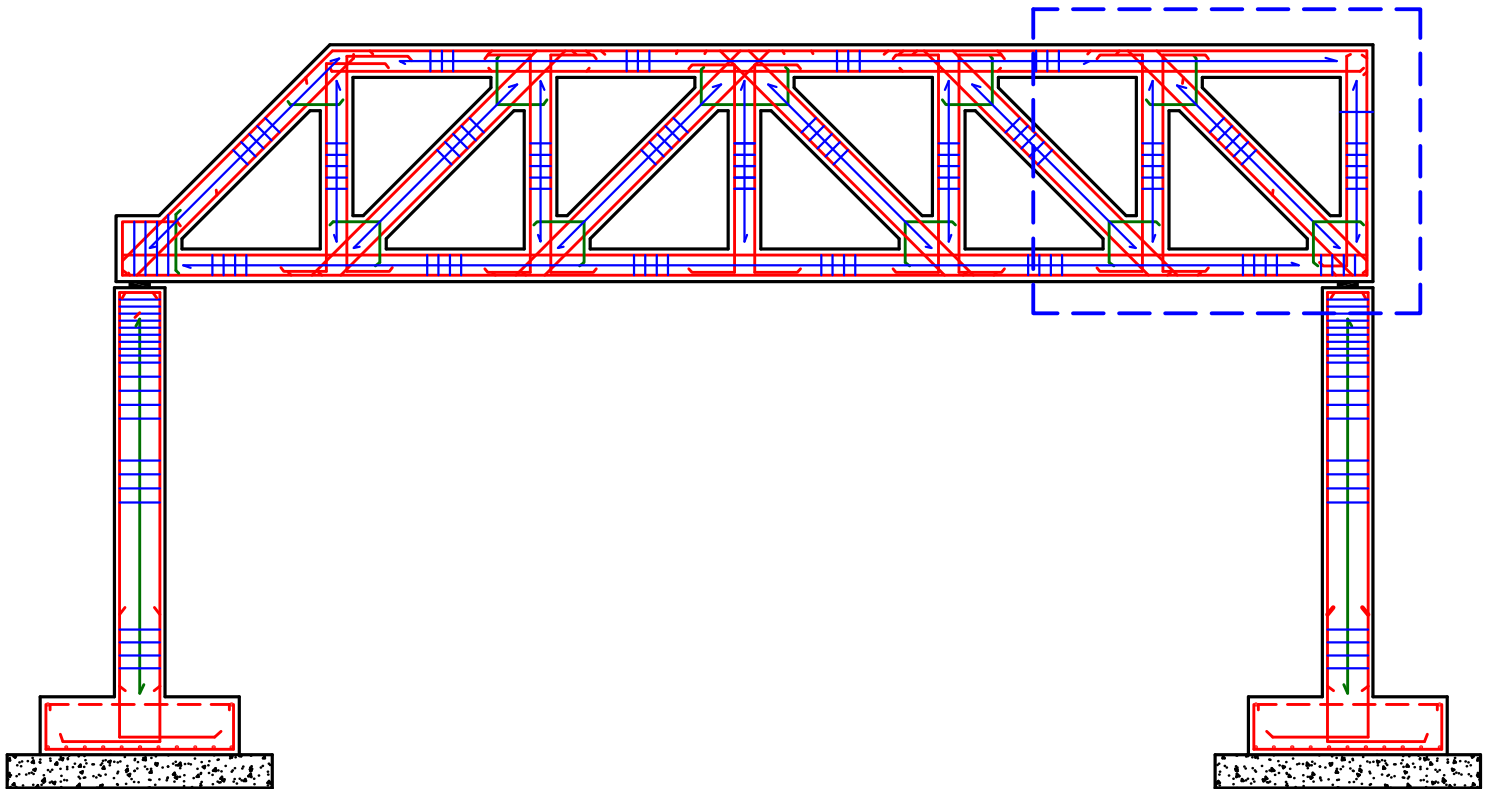
$2\phi 10 \setminus 30 \text{ cm}$
 $2\phi 10 \setminus 30 \text{ cm}$

ملحوظة

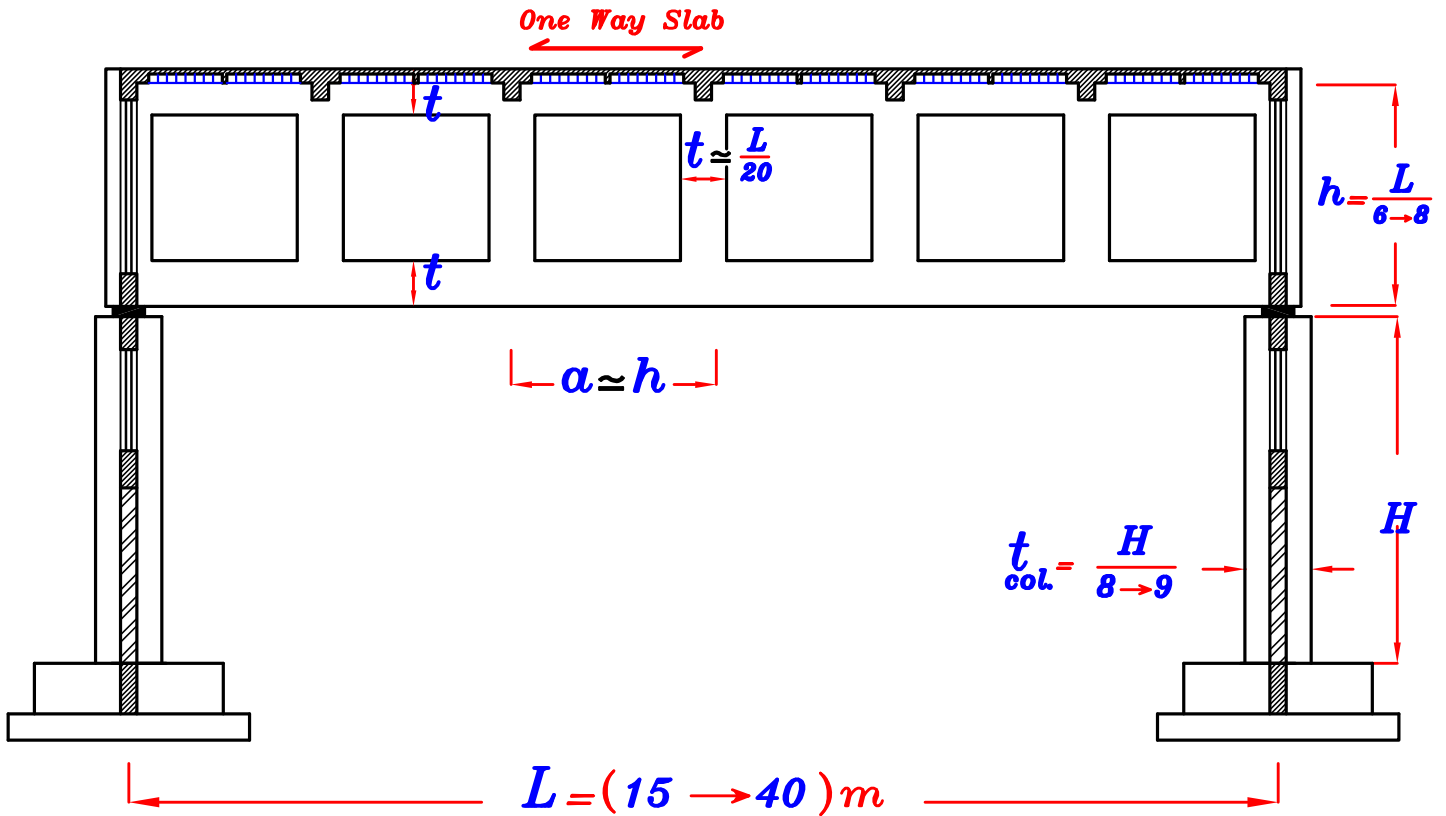
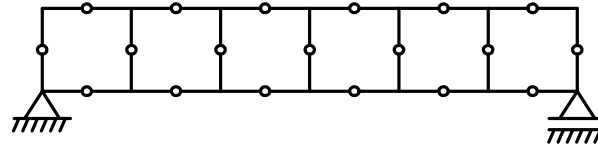
إتجاه ال **moment** غير معلوم لذا نصمم على
على أى إتجاه و نضع الحديد الأكبر فى الإتجاهين.



RFT. of Truss.



Vierendeel



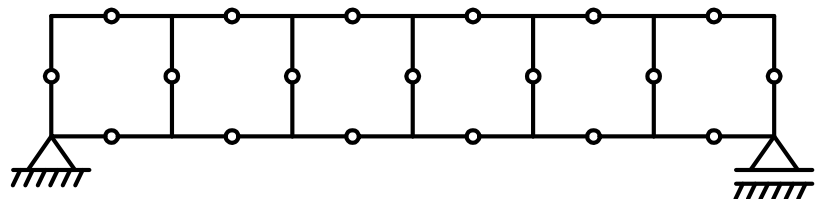
* Span (L) = $(15 \rightarrow 40) \text{ m}$

* Height (h) = $\frac{L}{6 \rightarrow 8}$

* t (Vierendeels) $\approx \frac{L}{20}$

* $b = 0.30 \text{ m}$ } الأكبر
 $\frac{\text{Spacing}}{20}$

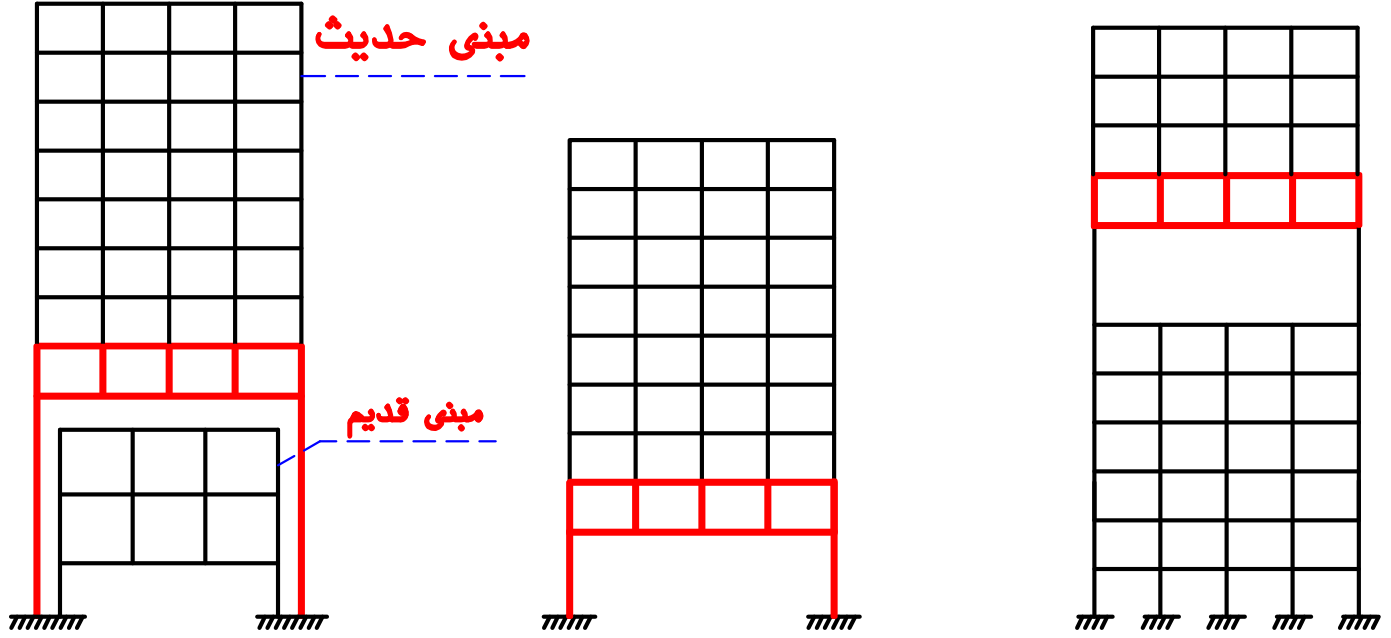
* $t_{col} = \frac{H}{8 \rightarrow 9}$



Statical System

أهم استخدامات ال *Vierendeels*

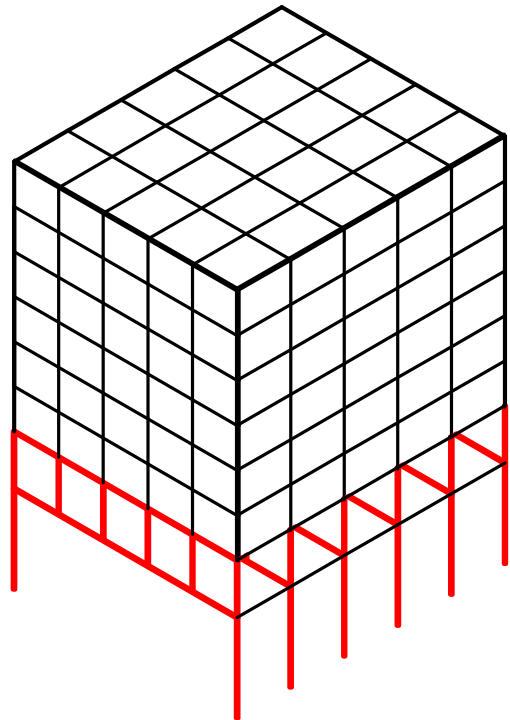
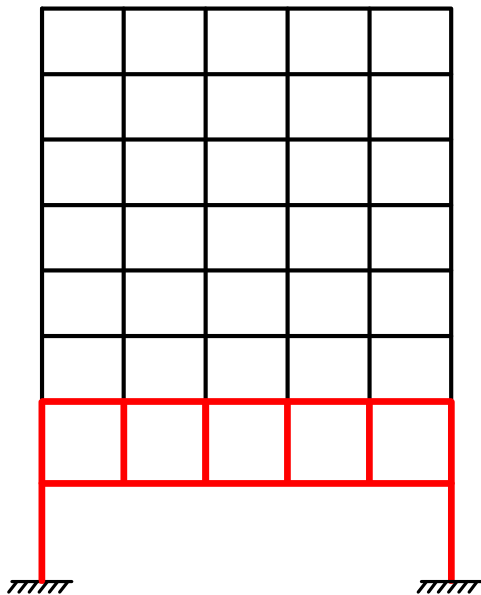
يتميز ال *Vierendeels* أنه يستطيع أن يحمل عدد من أدوار المبنى فوقه دون وضع أعمده في المنتصف .



المبنى الحديث محمول على *Vierendeels* و ال *Vierendeels* محموله على أعمده خارجيه دون أن يحمل على المبنى القديم

لا توجد أعمده في الدور الارضي لان كل الادوار العلويه محموله على *Vierendeels* و ال *Vierendeels* محموله على أعمده خارجيه

توجد قاعه بدون أعمده داخلية في الدور السادس و الادوار العلويه محموله على *Vierendeels* في الدور السابع و ال *Vierendeels* محموله على أعمده خارجيه



Analysis of Vierendeel.

We have Two method to solve the Vierendeel.

① Exact Method.

Using Computer

فى هذه الطريقه ممكن أخذ البلاطات

One way OR Two way

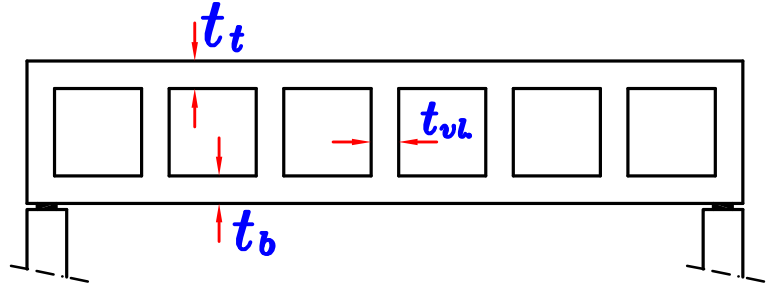
② Approximate Method.

To solve by this method we have to take

1- Take the slabs one way (at beam direction)

2- $t_t = t_b$

3- t_{vl} is Constant.

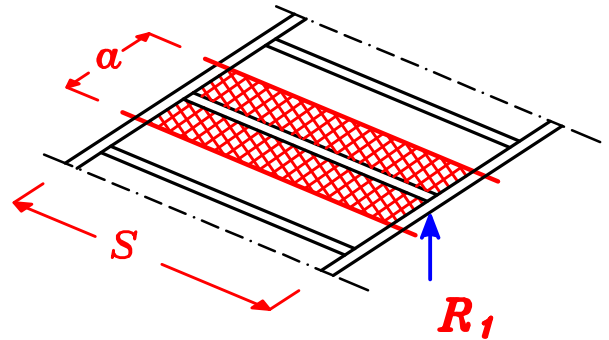


Steps of Design.

① Get Loads on Beam B_1

$$w_1 = 0.W_{(beam)} + w_s * a$$

$$R_1 = w_1 * S$$

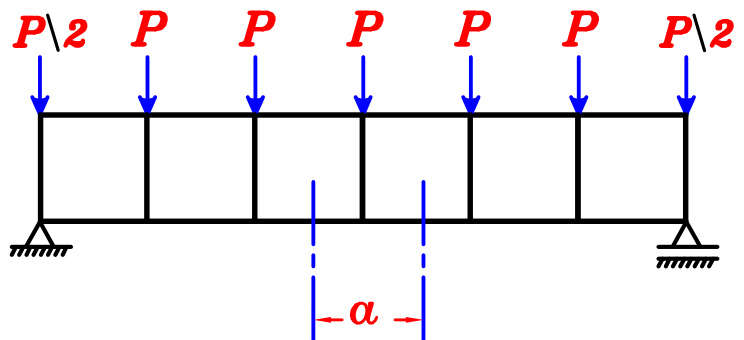


② Take

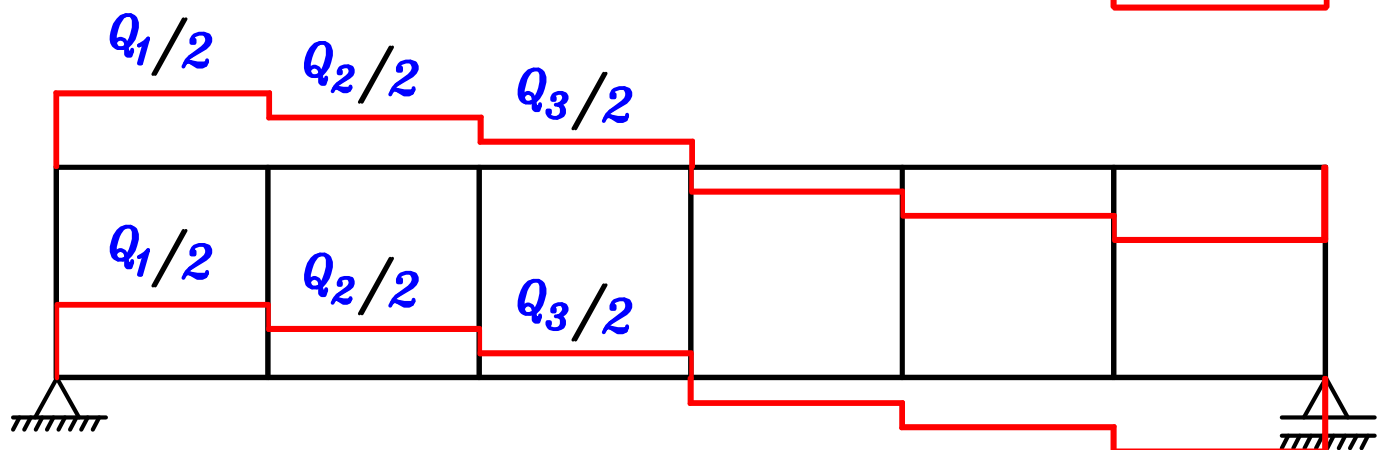
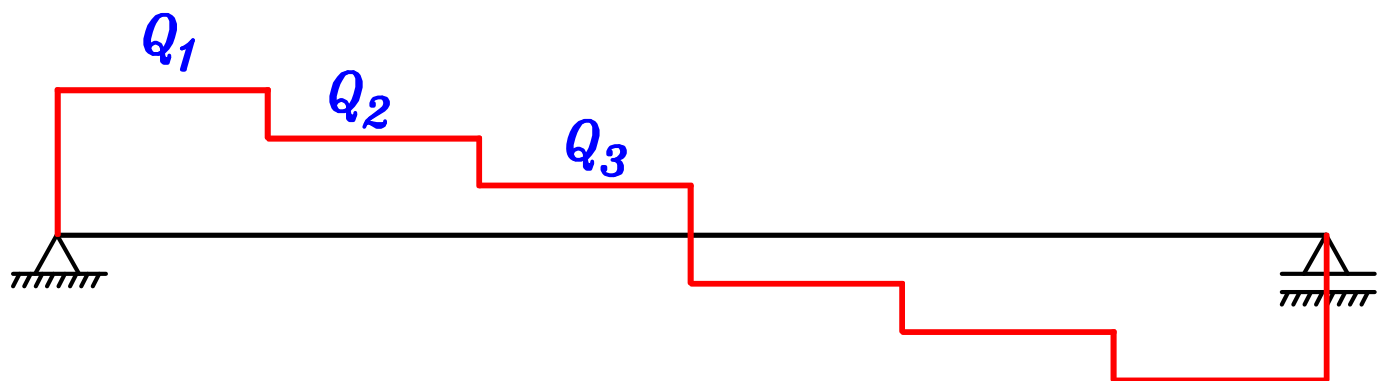
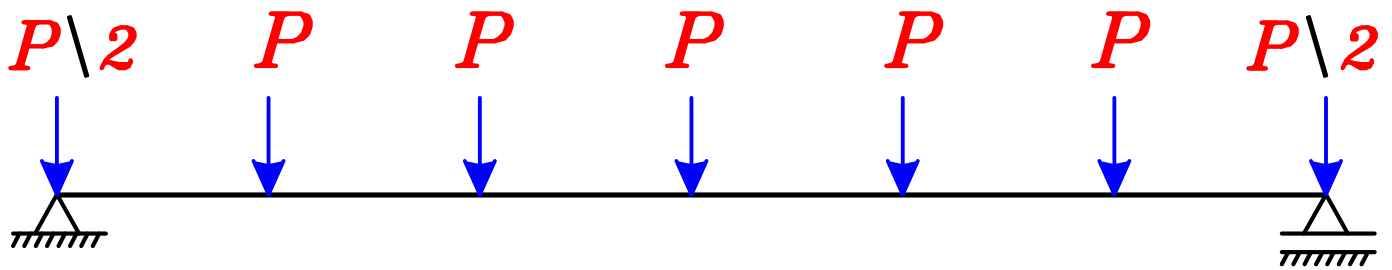
$$w' = 0.W_{(Vierendeel)} \\ \approx 25.0 \text{ kN/m (U.L.)}$$

$$P' = w' * a = \checkmark \text{ kN}$$

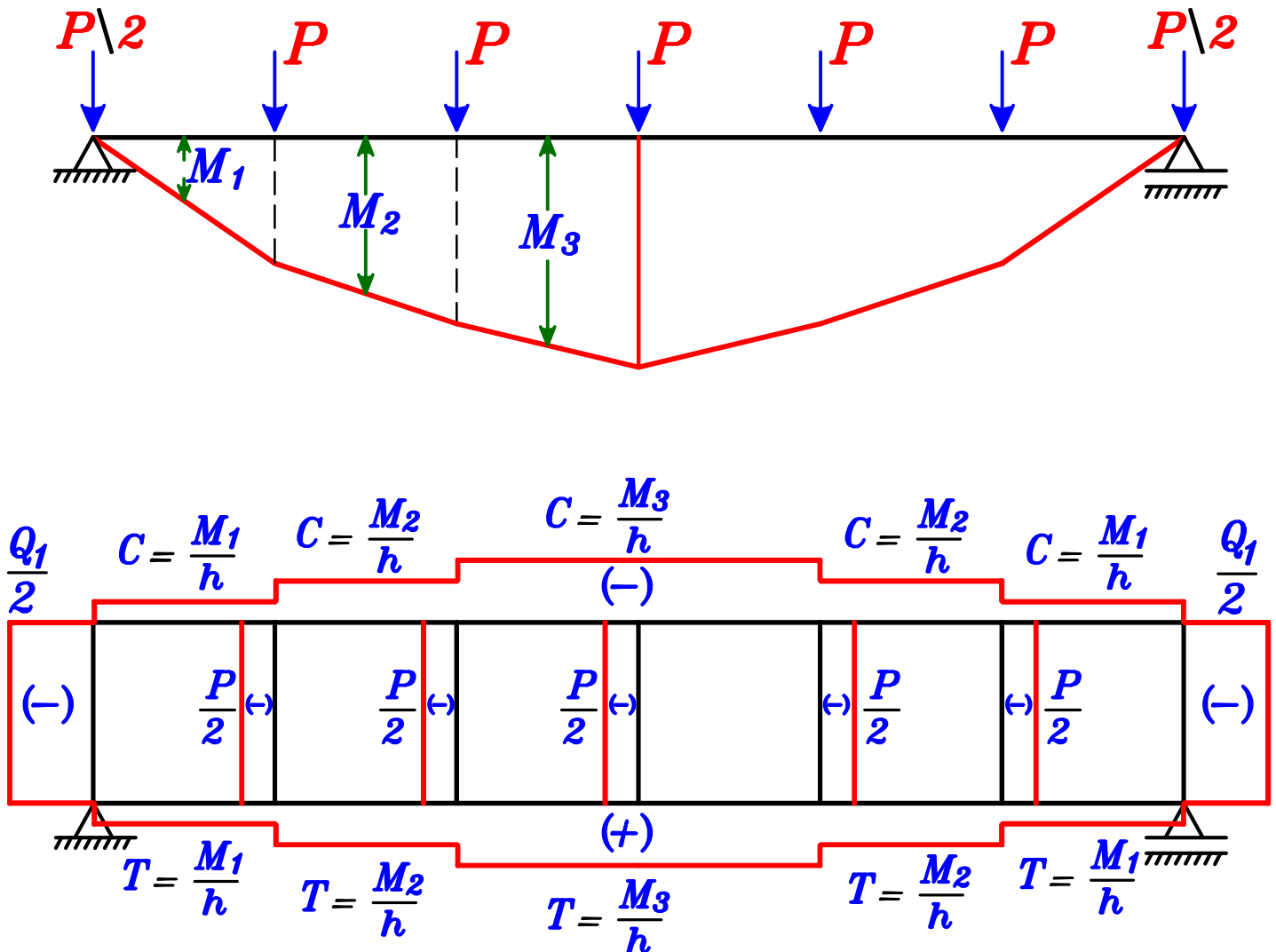
$$P = P' + R_1 = \checkmark \text{ kN}$$

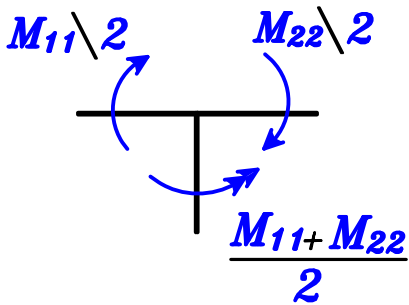
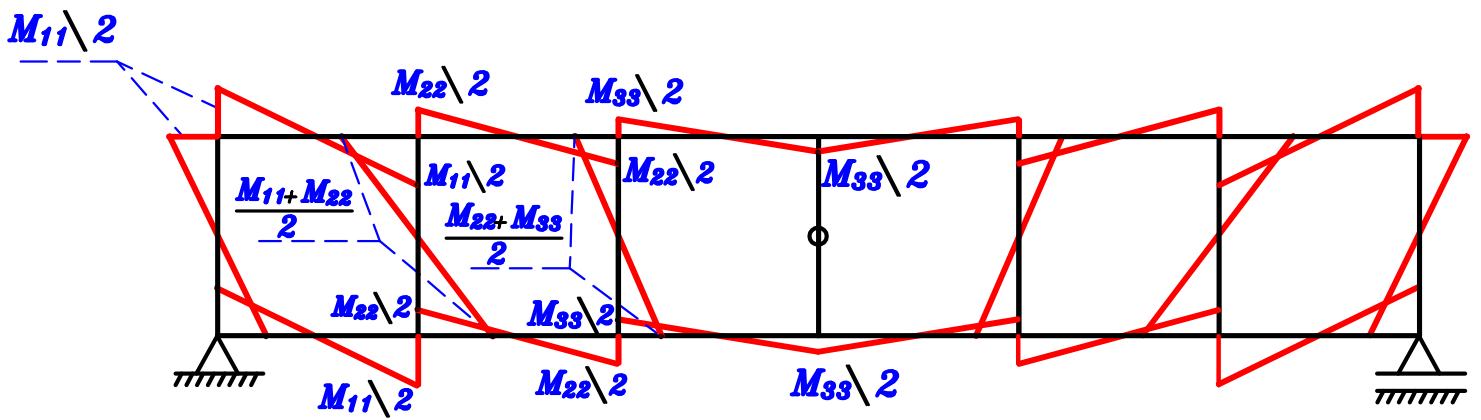
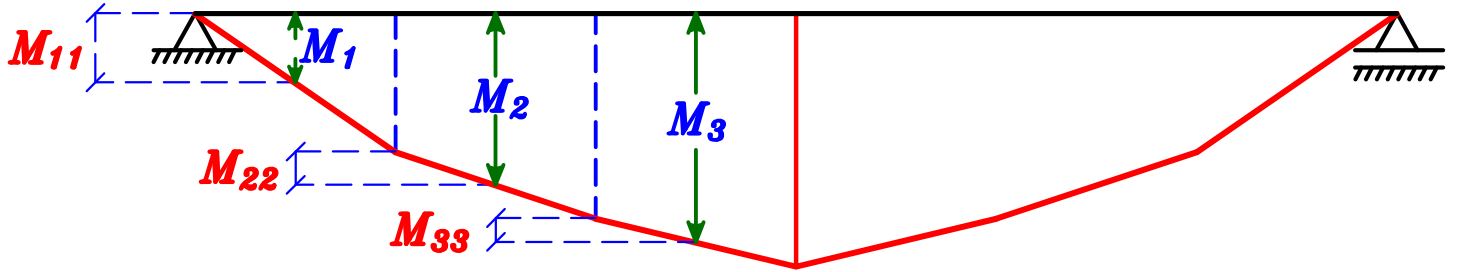


N.F.D. on Vierendeels.

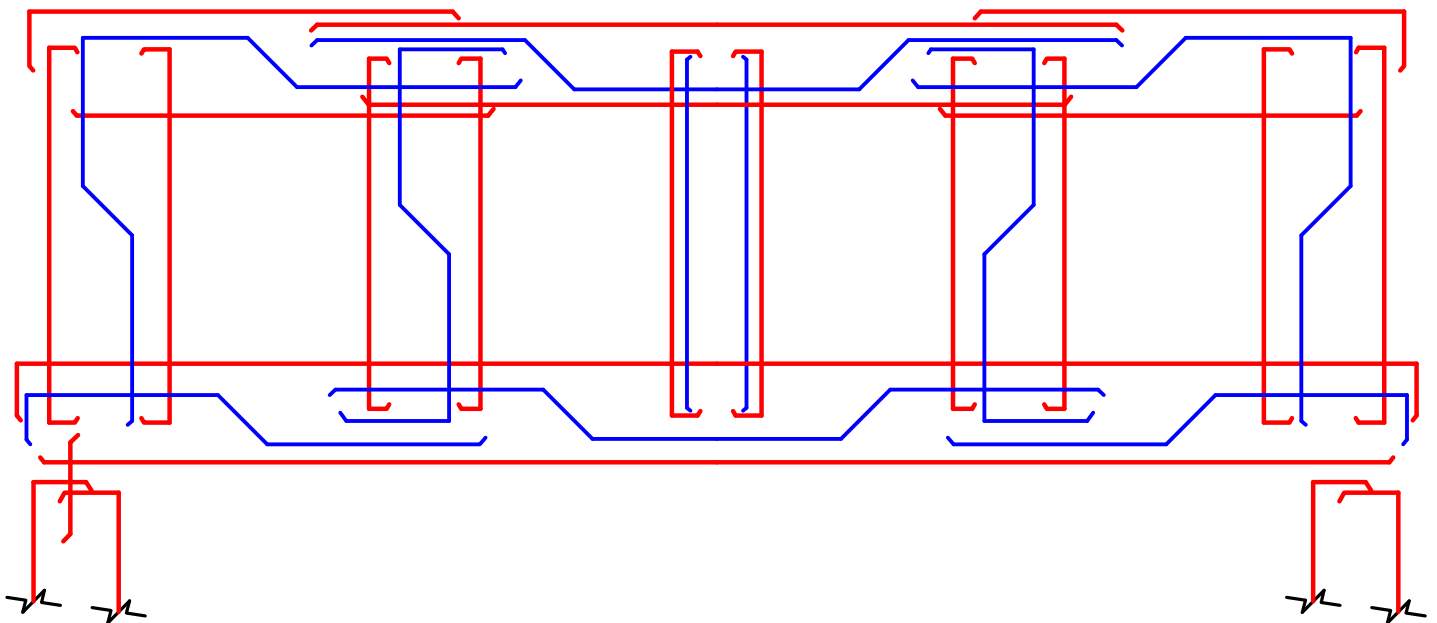
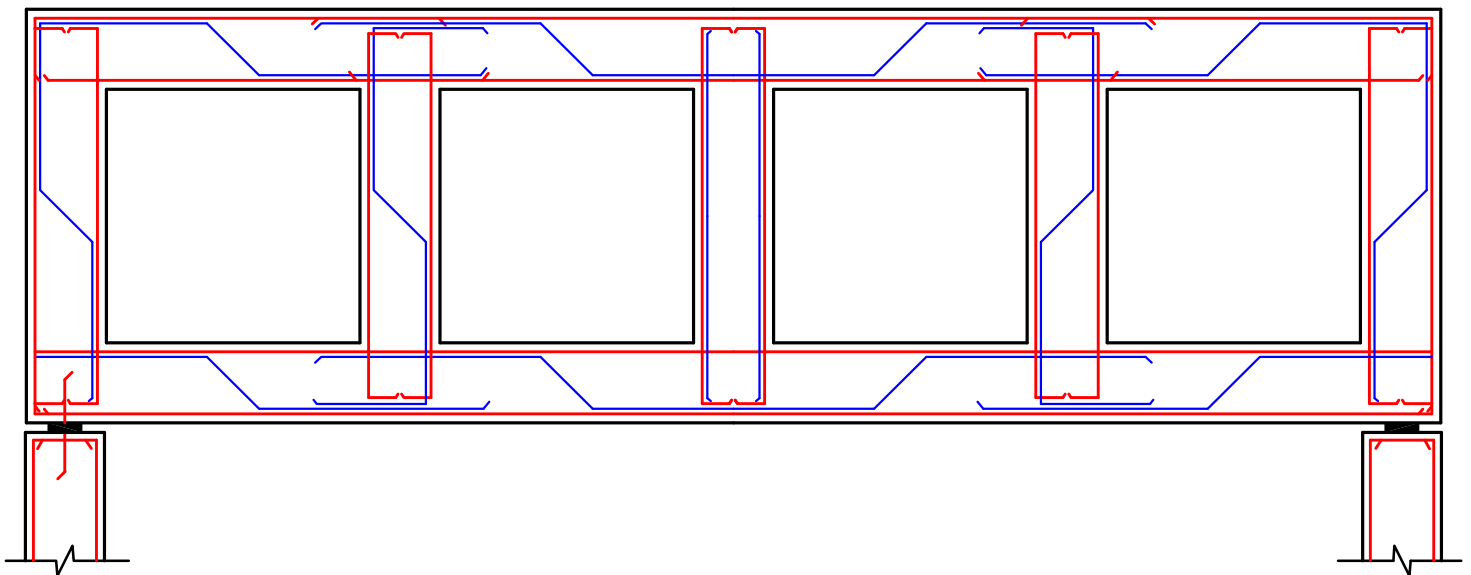
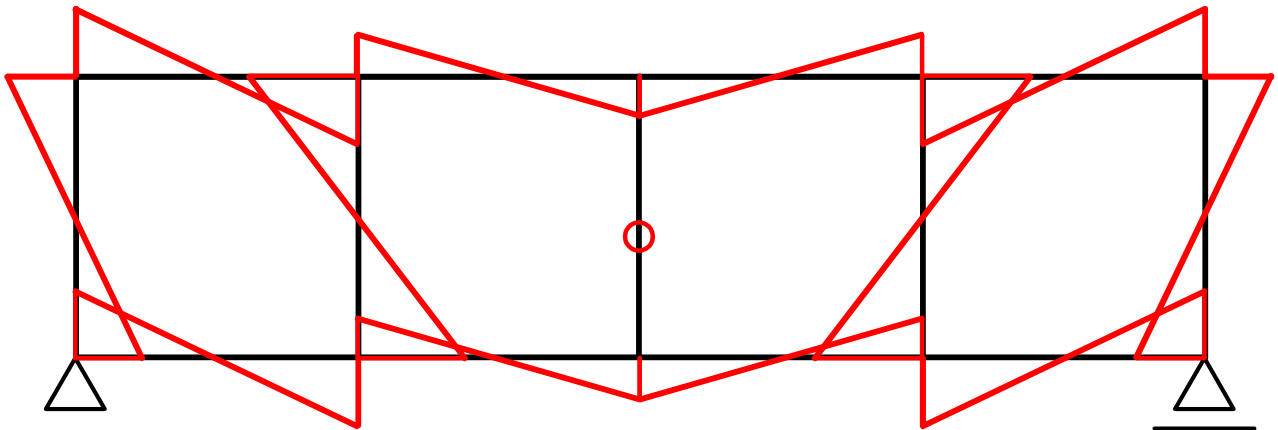


N.F.D. on Vierendeels.

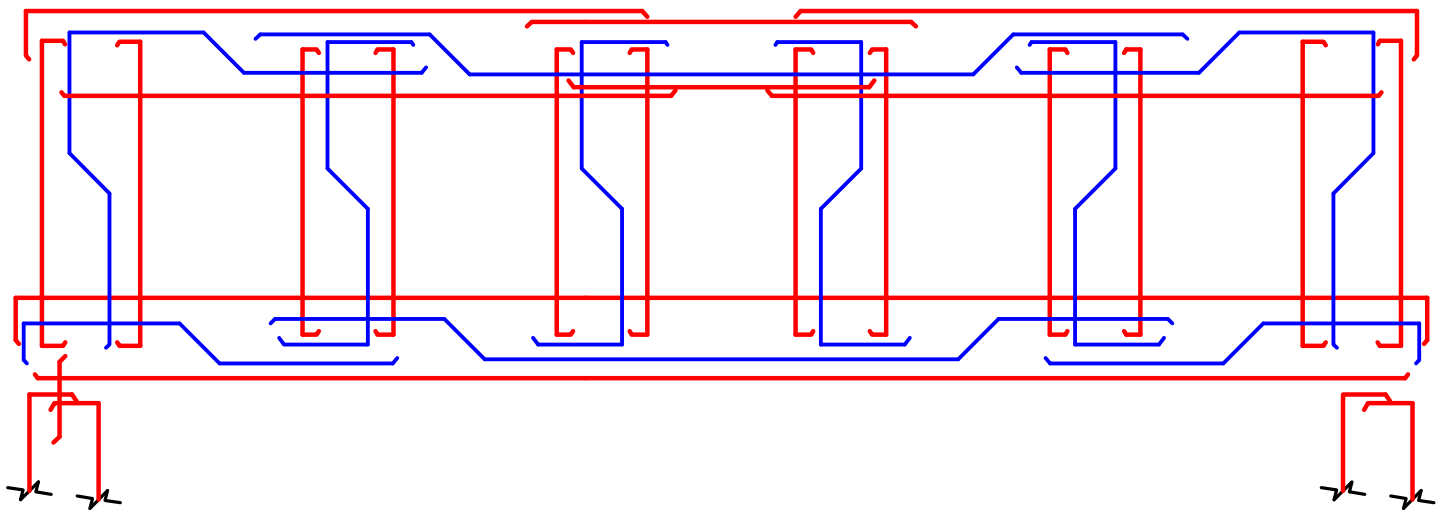
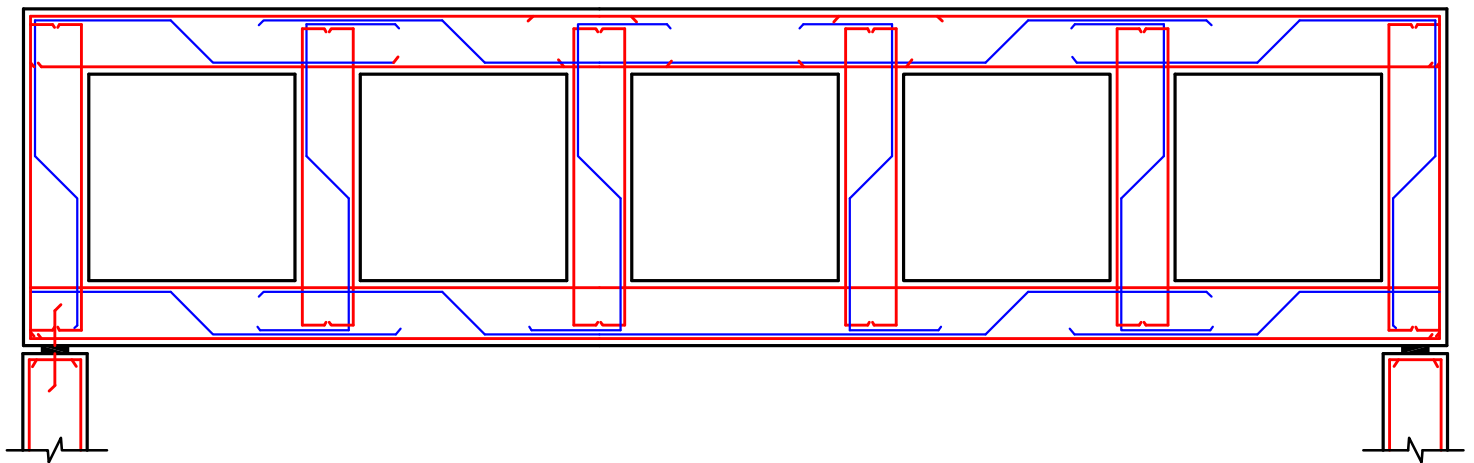
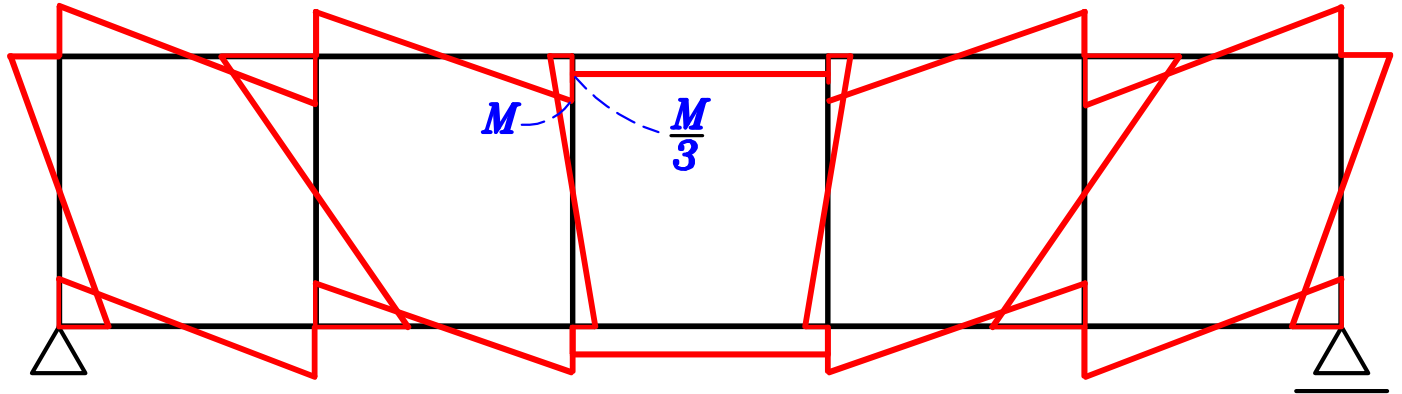




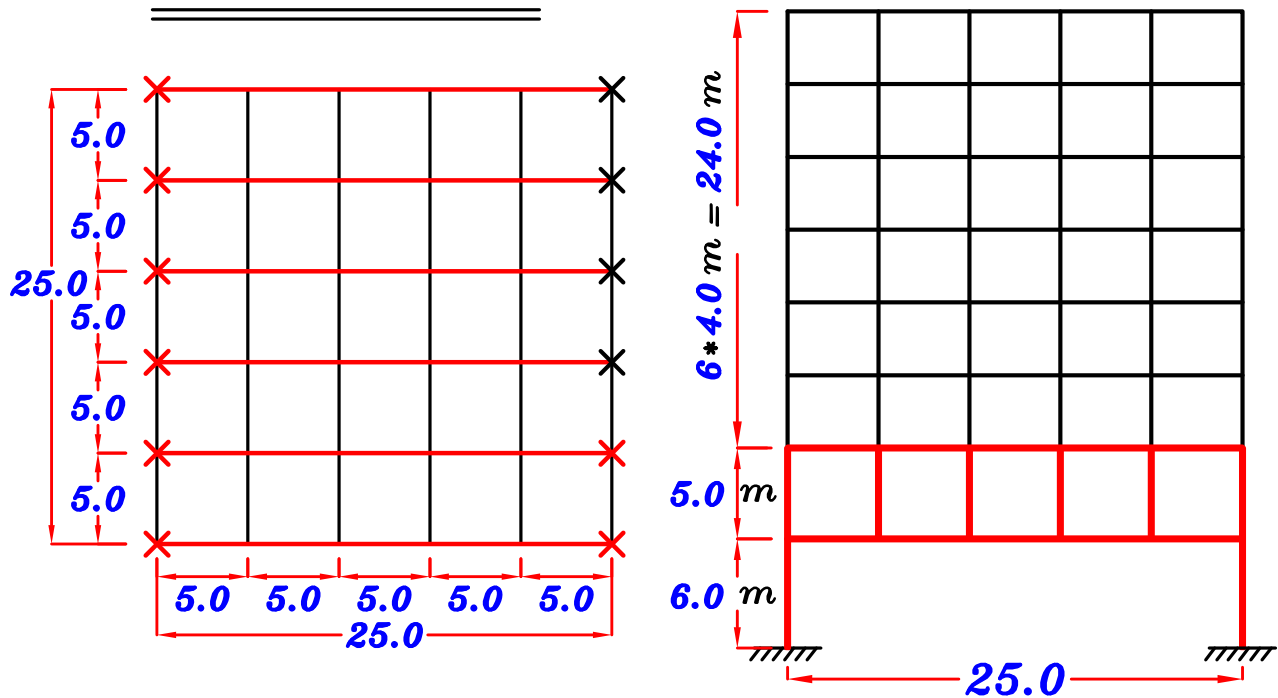
RFT. of Vierendeel. 4 Segments



RFT. of Vierendeel. 5 Segments



Example.



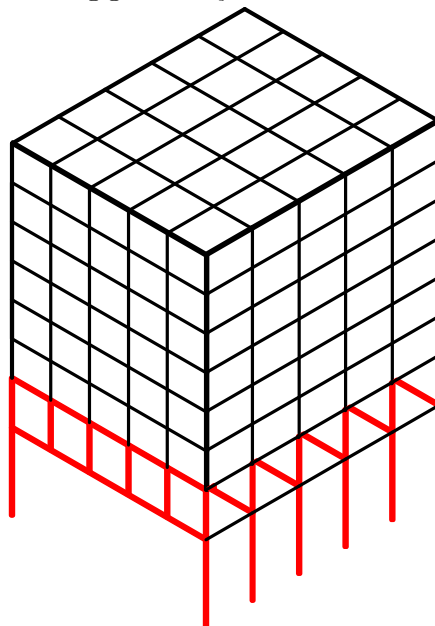
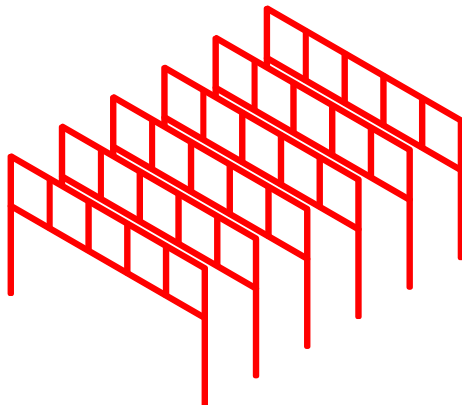
For the given Figure shows a layout of a building of an area $25.0 \times 25.0 \text{ m}^2$. The building consists of ground Floor and Seven typical Floor. The interior columns are removed at the ground Floor. The total equivalent working loads is 10.0 kN/m^2 .

$$F_{cu} = 30 \text{ N/mm}^2, \quad F_y = 360 \text{ N/mm}^2$$

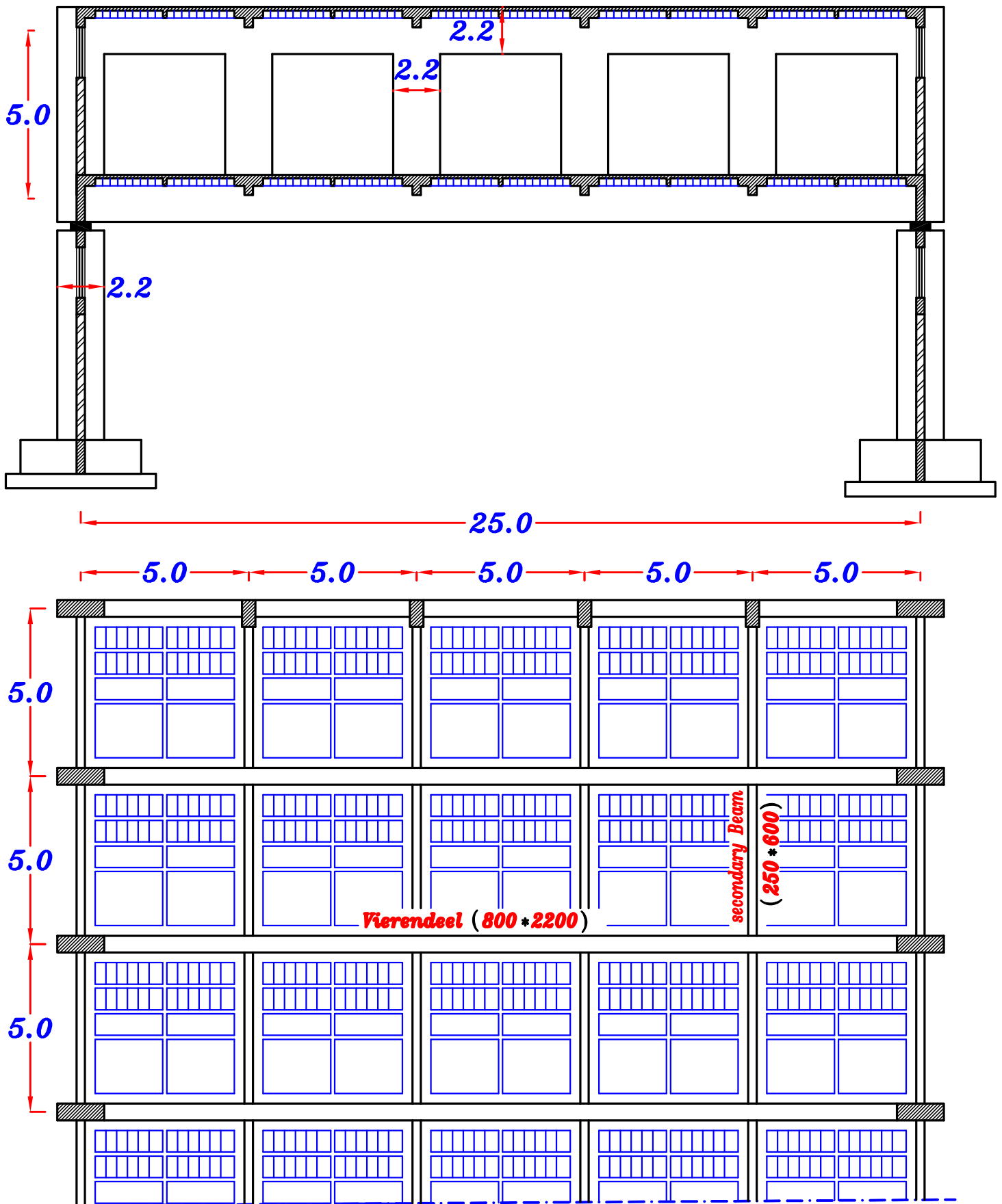
It is required to:

- 1- Choose a reasonable structural system For the ground Floor and draw its Concrete dimensions in plan and elevation to scale **1:50**
- 2- Calculate the Loads on the main supporting element.
- 3- Draw Internal Forces Diagrams For the main supporting element.
- 4- Design the main supporting element.
- 5- Draw details of RFT. of the main supporting element in elevation and cross sections to scale 1:25

Vierendeel



1 – Take the main supporting element *Vierendeel* (800 * 2200)



2- Calculate the Loads on the main supporting element.

The total equivalent working loads is **10.0 kN/m²**

$$- W_{av(u.L)} = 10.0 * 1.5 = \mathbf{15.0 \text{ kN/m}^2}$$

$$\begin{aligned} - \text{Total Load For one Floor} &= W_{av} * \text{Floor area} \\ &= \mathbf{15.0 * 25.0 * 25.0 = 9375 \text{ kN}} \end{aligned}$$

$$\begin{aligned} - \text{Total Load For the building} & \\ & \text{يتم زياده وزن سقف الدور الارضى .} \\ &= \text{Load of one Floor} * \text{No. of Floors.} \\ &= \mathbf{9375 * 8.0 = 75000 \text{ kN}} \end{aligned}$$

$$- \text{Total Load on One Vierendeel.}$$

يتم توزيع الحمل الكلى على عدد ال Vierendeels
مع فرض أن أول و آخر system سيحمل نصف الحمل فقط.

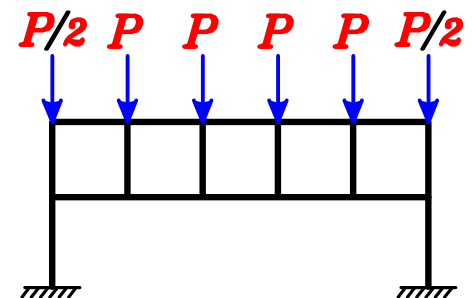
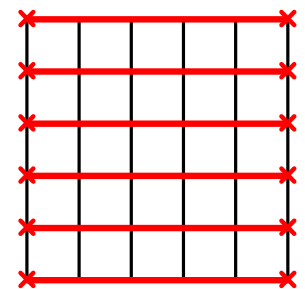
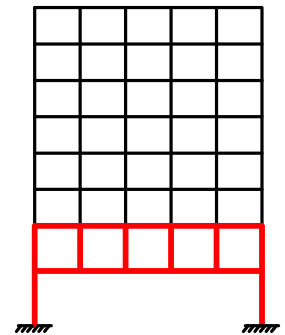
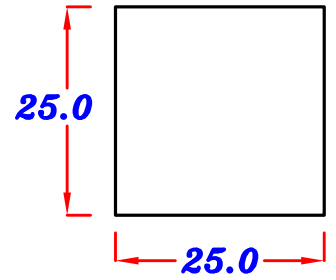
$$\text{Total Load on One Vierendeel.}$$

$$= \frac{\mathbf{75000 \text{ kN}}}{\mathbf{5.0}} = \mathbf{15000 \text{ kN}}$$

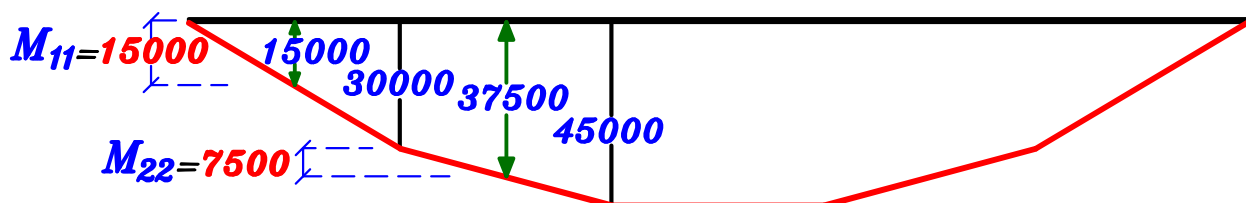
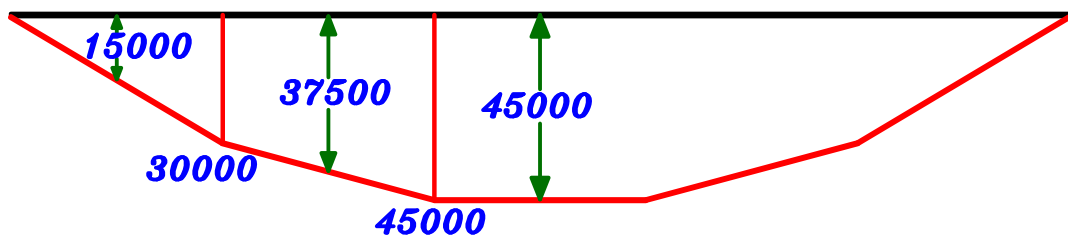
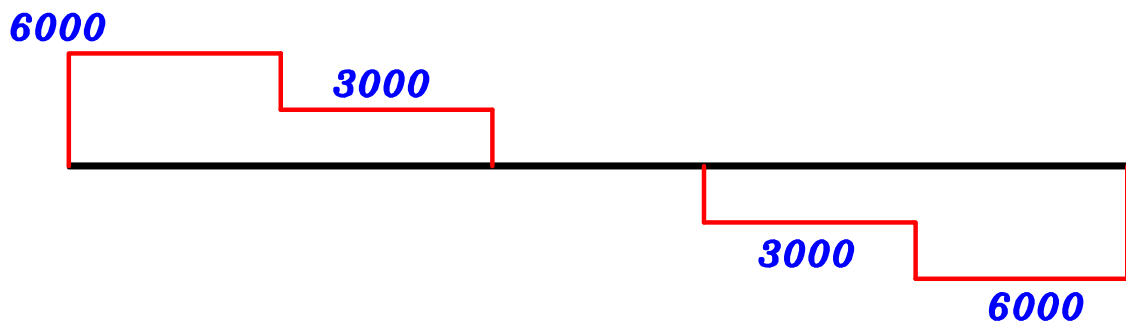
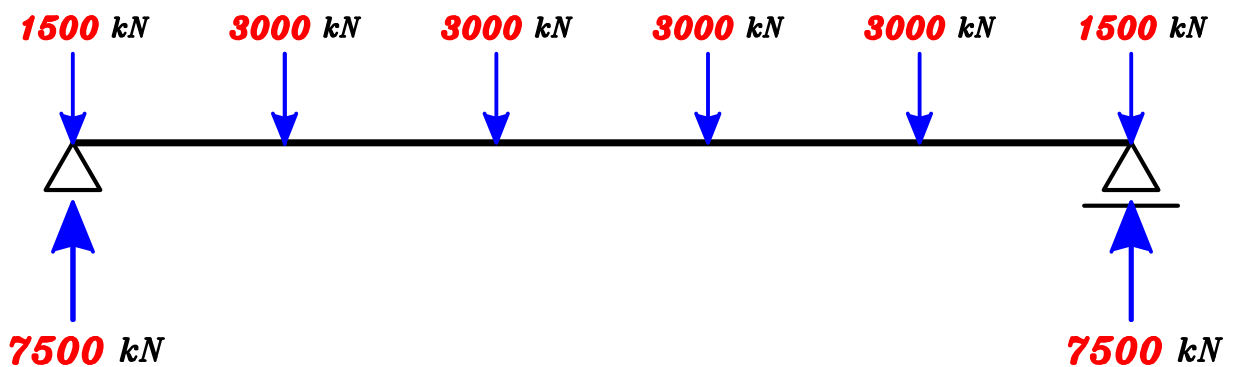
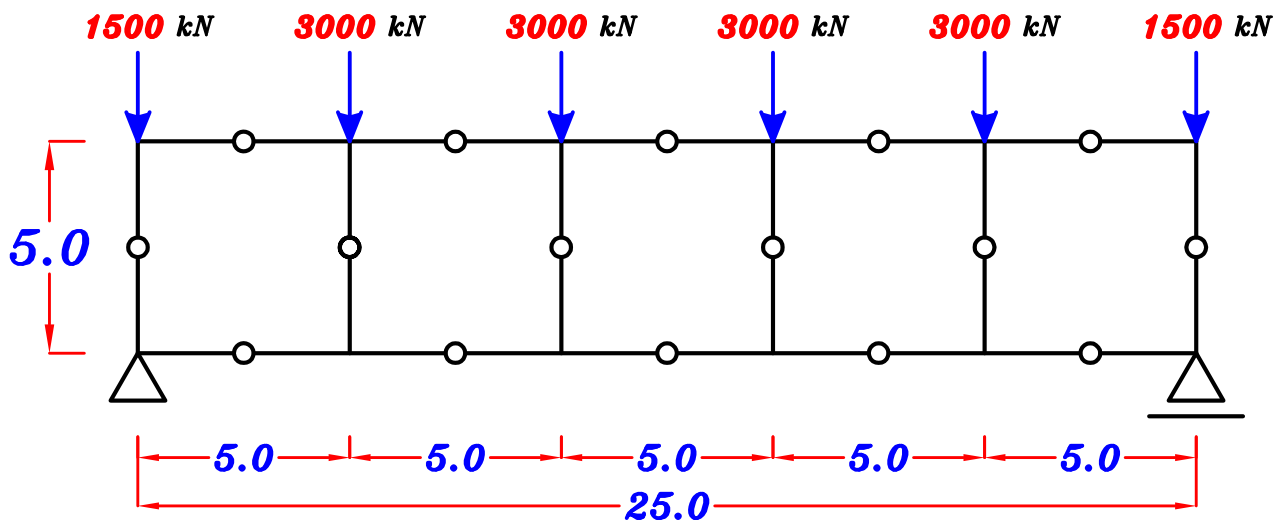
$$- \text{Load on one joint of the Vierendeel.}$$

يتم توزيع الحمل الكلى لل Vierendeels على عدد ال joints
مع فرض أن أول و آخر joint ستحمل نصف الحمل فقط

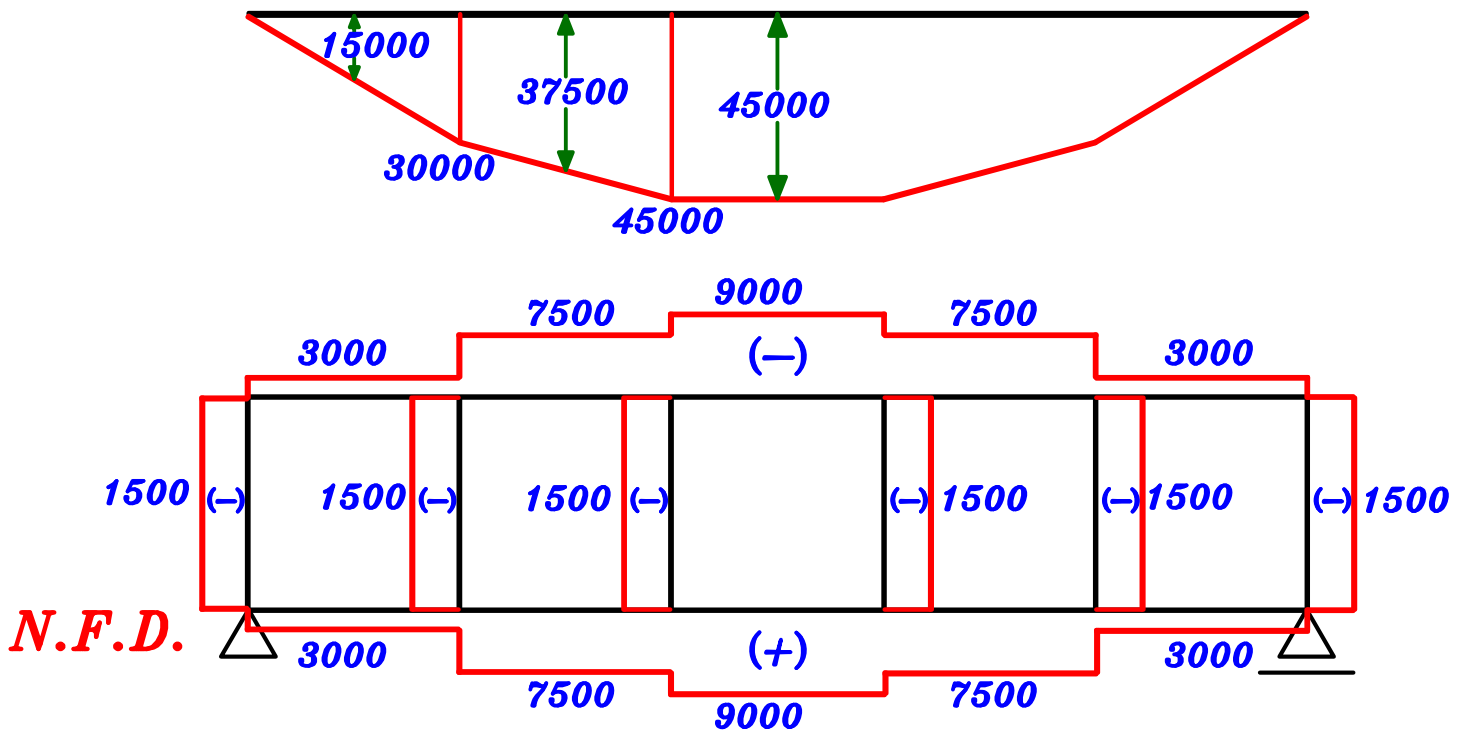
$$\mathbf{P} = \frac{\mathbf{15000 \text{ kN}}}{\mathbf{5.0}} = \mathbf{3000 \text{ kN (U.L.)}}$$



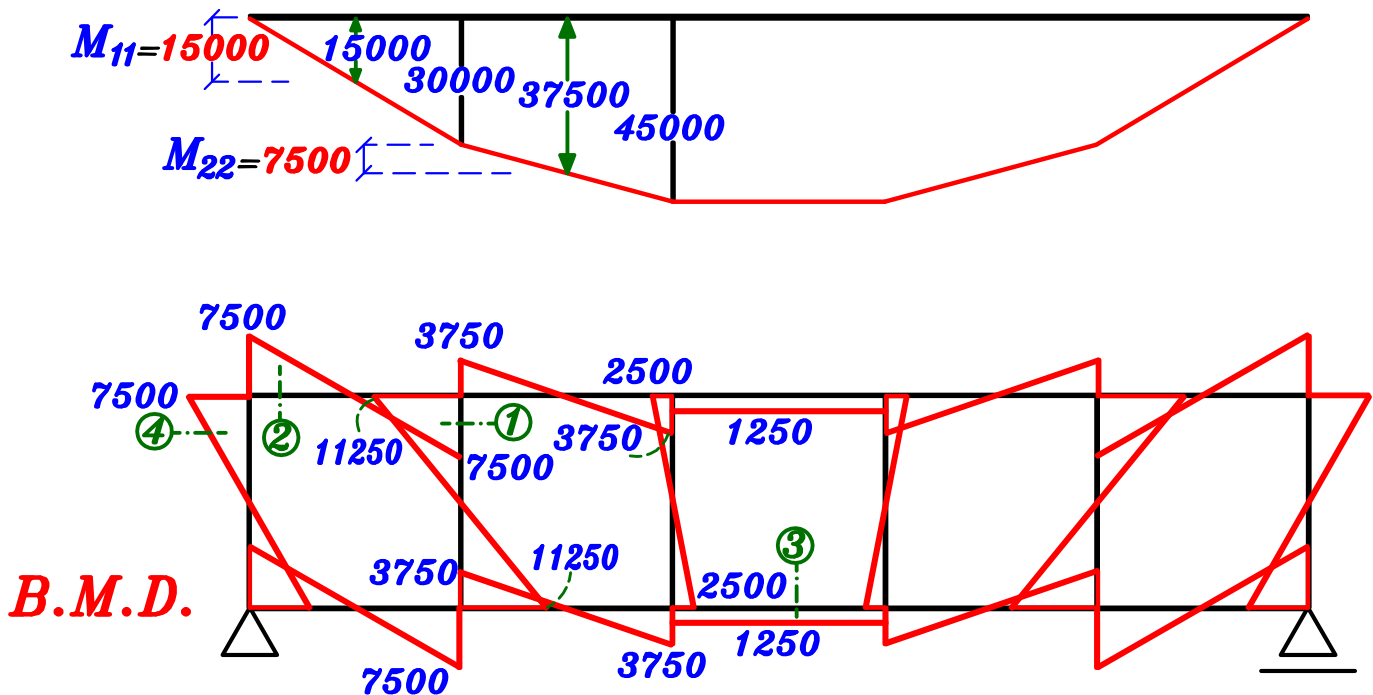
3– Draw Internal Forces Diagrams For the main supporting element.



N.F.D. on Vierendeel.



B.M.D. on Vierendeel.



Design of sections.

Sec. ① R-Sec.

$$M = 11250 \text{ kN.m} , N = 1500 \text{ kN} , b = 800 \text{ mm} , t = 2200 \text{ mm}$$

$$\text{Check } \frac{N}{F_{cu} b t} = \frac{1500 * 10^3}{30 * 800 * 2200} = 0.028 < 0.04 \quad (\text{Neglect } N)$$

$$2100 = C_1 \sqrt{\frac{11250 * 10^6}{30 * 800}} \rightarrow C_1 = 3.06 \rightarrow J = 0.747$$

$$A_s = \frac{M_{U.L.}}{J F_y d} = \frac{11250 * 10^6}{0.747 * 360 * 2100} = 19920 \text{ mm}^2$$

$$n = \frac{b - 25}{\phi + 25} = \frac{800 - 25}{32 + 25} = 13.6 = 13.0$$

26 ϕ 32

Sec. ② R-Sec.

$$M = 7500 \text{ kN.m} , N = 3000 \text{ kN} , b = 800 \text{ mm} , t = 2200 \text{ mm}$$

$$\text{Check } \frac{N}{F_{cu} b t} = \frac{3000 * 10^3}{30 * 800 * 2200} = 0.056 > 0.04 \quad (\text{Don't Neglect } N)$$

$$e = \frac{M}{N} = \frac{7500}{3000} = 2.50 \text{ m} \quad \therefore \frac{e}{t} = \frac{2.50}{2.2} = 1.13 \text{ m} > 0.5 \xrightarrow{\text{use}} e_s$$

$$e_s = e + \frac{t}{2} - c = 2.50 + \frac{2.2}{2} - 0.1 = 3.50 \text{ m}$$

$$M_s = N * e_s = 3000 * 3.50 = 10500 \text{ kN.m}$$

$$2100 = C_1 \sqrt{\frac{10500 * 10^6}{30 * 800}} \rightarrow C_1 = 3.17 \rightarrow J = 0.757$$

$$A_s = \frac{M_s}{J F_y d} - \frac{N_{U.L.}}{(F_y \setminus \delta_s)} = \frac{10500 * 10^6}{0.757 * 360 * 2100} - \frac{3000 * 10^3}{(360 \setminus 1.15)}$$

$$= 8764 \text{ mm}^2$$

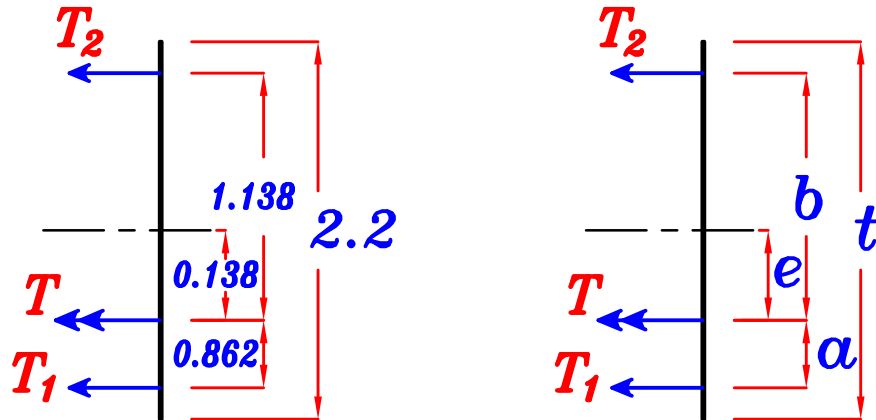
12 ϕ 32

Sec. ③ R-Sec.

$$M = 1250 \text{ kN.m} , T = 9000 \text{ kN} , b = 800 \text{ mm} , t = 2200 \text{ mm}$$

$$e = \frac{M}{T} = \frac{1250}{9000} = 0.138 \text{ m}$$

$$\therefore \frac{e}{t} = \frac{0.138}{2.20} = 0.062 < 0.5 \longrightarrow \text{Small Eccentricity.}$$



$$a = \frac{t}{2} - c - e = \frac{2.20}{2} - 0.10 - 0.138 = 0.862 \text{ m}$$

$$b = \frac{t}{2} - c + e = \frac{2.20}{2} - 0.10 + 0.138 = 1.138 \text{ m}$$

$$T_1 = T_{U.L.} \left(\frac{b}{a+b} \right) = 9000 \left(\frac{1.138}{0.862 + 1.138} \right) = 5121 \text{ kN}$$

$$A_{s1} = \frac{T_1}{(F_y / \phi_s)} = \frac{5121 * 10^3}{(360 / 1.15)} = 16358 \text{ mm}^2 \quad \text{22} \phi 32$$

Sec. ④ R-Sec.

$$M = 7500 \text{ kN.m} , N = 1500 \text{ kN} , b = 800 \text{ mm} , t = 2200 \text{ mm}$$

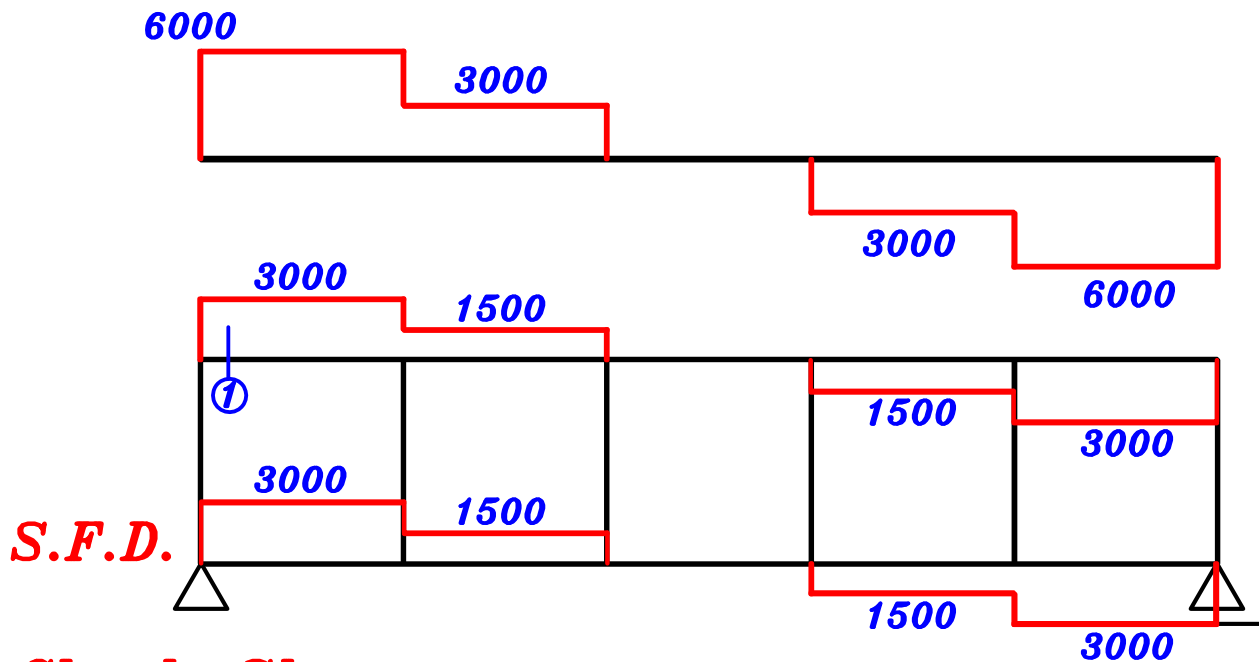
$$\text{Check } \frac{N}{F_{cu} b t} = \frac{1500 * 10^3}{30 * 800 * 2200} = 0.028 < 0.04 \quad (\text{Neglect } N)$$

$$2100 = C_1 \sqrt{\frac{7500 * 10^6}{30 * 800}} \longrightarrow C_1 = 3.75 \longrightarrow J = 0.793$$

$$A_s = \frac{M_{U.L.}}{J F_y d} = \frac{7500 * 10^6}{0.793 * 360 * 2100} = 12510 \text{ mm}^2$$

$$\text{16} \phi 32$$

S.F.D. on Vierendeels.



Check Shear.

– Allowable shear stress.

$$q_{cu} = 0.24 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.24 \sqrt{\frac{30}{1.5}} = 1.07 \text{ N/mm}^2$$

$$q_{max.} = 0.7 \sqrt{\frac{F_{cu}}{\delta_c}} = 0.7 \sqrt{\frac{30}{1.5}} = 3.0 \text{ N/mm}^2$$

Actual shear stress.

$$q_U = \frac{Q}{b d} = \frac{3000 * 10^3}{800 * 2100} = 1.78 \text{ N/mm}^2$$

$\therefore q_{cu} < q_U < q_{max.} \therefore$ We need Stirrups more Than $5 \phi 8 \setminus m$

Use Stirrups $\phi 12$ steel 360/520

$$\therefore \text{Use } q_s = q_u - \frac{q_{cu}}{2} = \frac{n A_s (F_y \setminus \delta_s)}{b S}$$

* Take $n = 4$, $\phi 12 \rightarrow A_s = 113 \text{ mm}^2$

$$1.78 - \frac{1.07}{2} = \frac{4 * 113 (360 \setminus 1.15)}{800 * S} \rightarrow S = 142.0 \text{ mm} > 100 \text{ mm}$$

$$\therefore \text{No. of stirrups} \setminus m = \frac{1000}{S} = \frac{1000}{142.0} = 7.0 \setminus m$$

Use Stirrups **7 $\phi 12 \setminus m$** **4** branches

